Direct observation of an attosecond electron wave packet in a nitrogen molecule

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Capturing electron motion in a molecule is the basis of understanding or steering chemical reactions. Nonlinear Fourier transform spectroscopy using an attosecond-pump/attosecond-probe technique is used to observe an attosecond electron wave packet in a nitrogen molecule in real time. The 500-as electronic motion between two bound electronic states in a nitrogen molecule is captured by measuring the fragment ions with the same kinetic energy generated in sequential two-photon dissociative ionization processes. The temporal evolution of electronic coherence originating from various electronic states is visualized via the fragment ions appearing after irradiation of the probe pulse. This observation of an attosecond molecular electron wave packet is a critical step in understanding coupled nuclear and electron motion in polyatomic and biological molecules to explore attochemistry.

INTRODUCTION

In chemistry, we seek to understand how chemical bonds form or break to control reactions or create new substances. The proton and electron transfer processes are well-known fundamental processes in photocatalysis and photosynthesis reactions (1, 2). Until now, ultrafast molecular dynamics has been investigated using two complementary approaches, namely, diffraction (3, 4) and spectroscopic methods (5–7). Time-resolved electron or x-ray diffraction can reveal the ensemble-averaged temporal evolution of nuclear and/or charge distributions in molecules. However, the temporal resolution is currently in the femtosecond range. The spectroscopic method enables us to investigate temporal evolution of nuclear and/or charge distributions in a single molecule.

With the recent advent of attosecond extreme ultraviolet pulses, research in observing and controlling ultrafast electronic motion in atoms and molecules in real time has been realized (8, 9). Thus far, the sub-femtosecond chemical reactions of a small molecule are controlled by inducing the charge localization using the carrier envelope phase-stabilized few-cycle pulse (5, 10, 11) or visualized by the correlated wave packet pairs (12). Correlated electron dynamics on the attosecond time scale have only been investigated in atomic targets (13, 14). Although some valuable insights on attosecond molecular response have been obtained without using attosecond pulses (15, 16), it is beyond doubt that the attosecond-pump/attosecond-probe method is the most direct and universal method to extract attosecond molecular dynamics (17, 18). To realize the attosecond-pump/attosecond-probe measurement, however, an intense attosecond pulse is required to achieve a focal intensity larger than 1014 W/cm2 (19–21).

In the new research field of attochemistry, the electronic motion in a molecule will be manipulated before the onset of nuclear vibrational motion (8). This indicates that the chemical reactions should be steered within the time scale of electrons. Because the spectral bandwidth of an attosecond pulse covers energy levels of multiple electronic states, multiple states can be excited coherently to create an electron wave packet (EWP). Moreover, the generation process of an attosecond pulse via the high-harmonic generation (HHG) (22) itself intrinsically creates the EWP, and it is considered to be one of the straightforward ways to observe the molecular EWP on the attosecond time domain, but it is difficult to specify the relevant electronic states because the HHG process is induced by the highly nonlinear process of tunneling ionization and the strong driving light pulse perturbs the electronic states.

When the EWP is prepared between two electronic states with energy gap ∆E, the coherent oscillation between the two states occurs with a period of 2π/∆E. Thus far, several probe schemes for observing molecular EWP have been proposed, and these schemes are based on photoelectron spectroscopy (23, 24) or high-harmonic (25, 26) spectroscopy. In the case of photoelectron spectroscopy, the probe pulse ionizes the electronic states forming the EWP to the same continuum state. Thus, the spectral bandwidth of the probe pulse must cover ∆E.

In contrast, here we present the direct observation of temporal evolution of the EWP in a nitrogen molecule by the attosecond-pump/attosecond-probe method using nonlinear Fourier transform spectroscopy (NFTS) (27). The scheme for observing the EWP in N2 is shown schematically in Fig. 1A. The potential energy curves of electronic states relevant to the EWP formation are shown in Fig. 1B with the harmonic and dephasing distribution of a few-cycle attosecond pulse train (APT) composed of a few attosecond pulses in the envelope. The pump pulse creates a coherent EWP among the bound electronic states in N2 and N2+. Note that the latter involves the ejection of a photoelectron. The probe pulse excites all electronic states involved in the EWP to respective dissociative electronic states in N2+ and triggers fragmentation to generate the N+ ion. The pump-probe delay-dependent kinetic energy (KE) distribution of N+ exhibits at least four characteristic oscillations from 500 as to 3.5 fs ascribed to the electronic motion or charge oscillation between two electronic states.

In the proposed method, the KE of the fragment ion is a measure of the EWP. We first discuss the coherent motion of the EWP created in the N2+ electronic states. The pump pulse ionizes to create a superposition of two bound electronic states in N2+, namely, an EWP. The probe pulse with delay δt excites this EWP to another coherent superposition of multiple dissociative electronic states, in which N2+ dissociates into N+ + N. There are several quantum pathways in the present pump-probe study that lead to the ejection of N+ with the same KE. These pathways allow us to observe the temporal evolution of the EWP. Therefore, when...
we scan the delay $\Delta t$ and record the fragment $N^+$ with an appropriate KE, a periodic modulation of the ion yield associated with the temporal evolution of the EWP appears because of the coherence of quantum pathways.

We have also observed a coherent motion of the EWP created between an electronic state in $N_2$ and an electronic state in $N_2^+$. The probe process in this case is similar to that described above. The only difference is that the excitation process with the probe pulse accompanies the ionization of $N_2$ to induce dissociations. This is described in detail in section 2 of the Supplementary Materials.

RESULTS

Vibrational wave packet assignment

We conducted an NFTS measurement to observe the attosecond electronic responses by scanning the delay $\Delta t$ between the pump-APT and the probe-APT (the experimental setup is described in Materials and Methods). Figure 2A shows the delay-dependent $N^+$ signals at a KE, $E = 0.2$ eV. Figure 2B shows the Fourier power spectrum of Fig. 2A, which exhibits four peaks from 500 as to 3.5 fs. The observed frequency peaks are ascribed to the vibrational period of $N_2$. As shown schematically in Fig. 3C, peaks B and C originate from $N^+$ generated by the excitation with the 11th- and higher-order harmonics at the outer turning point to the $3^2\Sigma_g^+$ state and dissociate into different dissociation limits ($L_4$ for peak B and $L_3$ for peak C). On the other hand, peaks D and E originate from $N^+$ generated by the excitation with the 13th- and higher-order harmonics at the inner turning point to the $3^2\Sigma_g^+$ state and dissociate into different dissociation limits ($L_4$ for peak D and $L_3$ for peak E). The weak peak A around $E = 0.2$ eV is assigned to $N^+$ generated by the excitation with the seventh- or higher-order harmonics at the inner turning point to the $3^2\Sigma_g^+$ state, and the probe scheme of each peak is shown in Fig. 3D. The observed nuclear motions $T_{\text{vib}} = 15$ to 20 fs (50 to 67 THz) are assigned to the VWP in the electronic states in $N_2$. Peaks G to I in Fig. 3B originate from the VWP of the $A^3\Pi_u$ state, and the probe scheme of each peak is shown in Fig. 3D. Peak F around $E = 0.2$ eV originates from $N^+$ generated by the excitation with the fifth-order harmonic to the $D^3\Pi_g$ state and dissociates into $L_1$. The observed nuclear motions $T_{\text{vib}} = 20$ to 70 fs (50 to 180 THz) are assigned to the VWP in the electronic states in $N_2$. Peaks G to I in Fig. 3B originate from the VWP of the $A^3\Pi_u$ state, and the probe scheme of each peak is shown in Fig. 3D. Peak F around $E = 0.2$ eV originates from $N^+$ generated by the excitation with the fifth-order harmonic to the $D^3\Pi_g$ state and dissociates into $L_1$. On the basis of the VWP measurement, we found that five electronic states ($b^1\Sigma_u^+, X^2\Sigma_g^+, A^3\Pi_u, B^3\Sigma_g^+$, and $C^2\Sigma_g^+$) can be probed to generate $N^+$.
with the same KE of 0.2 eV (see sections 3 and 4 in the Supplementary Materials). In the above VWP assignment, it is difficult to absolutely exclude the existence of other dissociation channels because the assignment is based on the calculated potential energy curves of highly excited electronic states.

EWP assignment

We will now assign the peaks shown in Fig. 2B to the EWP created on pairs of electronic states. Peak 4, which exhibits the fastest oscillation at $T_{\text{EWP}} = 500 \text{ as}$ ($\Delta E = 8.3 \text{ eV}$), can be ascribed to the EWP created between the $A^2\Pi_u$ and $C^2\Sigma^+_g$ states. The oscillation period $T_{\text{EWP}} = 3.5 \text{ fs}$ ($\Delta E = 1.2 \text{ eV}$) for peak 1 is ascribed to the EWP between the $X^2\Sigma^+_g$ and $A^2\Pi_u$ states. On the other hand, peaks 2 and 3 can be ascribed to the EWP between the electronic state in $N_2$ and the electronic state in $N_2^-$.

Figure 2D can be ascribed to the difference in the transition probabilities. The temporal evolution of the differential electron density map (EDM) between the $A^2\Pi_u$ and $C^2\Sigma^+_g$ states shown in Fig. 4C reveals the transition probabilities for ($X^2\Sigma^+_g \rightarrow A^2\Pi_u$) and ($B^2\Sigma^+_u \rightarrow C^2\Sigma^+_g$) are considered to be major contributions because the transition probabilities for ($X^2\Sigma^+_g \rightarrow B^2\Sigma^+_u$) are much smaller than those for ($b^1\Sigma^+_u \rightarrow A^2\Pi_u$) and ($b^1\Sigma^+_u \rightarrow C^2\Sigma^+_g$). Figure 2C shows the frequency spectrogram calculated from the nuclear correlation function $\text{Re} \left[ \sum_{i<j} \Psi^*(k, \Delta t) \Psi_j(R, \Delta t) \right]$, where $\Psi_j(R, \Delta t)(k = i, j)$ are the nuclear wave functions. The Fourier transform of Fig. 2C is shown in Fig. 2D, and it qualitatively reproduces the experimental result shown in Fig. 2B. The discrepancy in the relative intensity of peaks between the experimental result shown in Fig. 2B and the numerical simulation shown in Fig. 2D can be ascribed to the difference in the transition probabilities.

The temporal evolution of the differential electron density map (EDM) between the $A^2\Pi_u$ and $C^2\Sigma^+_g$ states shown in Fig. 4C reveals the variation of the electron spatial distribution where the reference electron density is set to that of $X^2\Sigma^+_g$ state (see section 5 in the Supplementary Materials). The EDM oscillates with a period of 500 as, and the nuclear motion on this time scale is negligible. Thus, the distributions at $\Delta t = 0$ as and $\Delta t = 500$ as are identical, and the distribution at $\Delta t = 250$ as is also the same, but with opposite phase. However, the EDM at $\Delta t = 9000$ as is similar to that at $\Delta t = 125$ as because both the nuclear correlation functions are almost zero.

CONCLUSION

Here, we observed the EWP among five bound electronic states in $N_2$ using the attosecond-pump/attosecond-probe method by detecting fragment ions.
as a good measure of electron motions. The pump and probe processes of the EWP among these five electronic states are securely identified by measuring the coherent temporal evolution of the VWP in each electronic state. The combination of an intense a-few-pulse APT with a moderate spectral bandwidth and NFTS makes it possible not only to visualize attosecond electron motion in molecules but also to assign electronic states. Compared with conventional methods (23–26) for observing EWP, the proposed approach has distinct advantages in that (i) the probe process of each electronic state can be unambiguously identified, (ii) the eigenenergy of final states excited by the probe pulse can be different for each electronic state, and (iii) the EWP formed in the singly charged electronic states can be probed without further ionization to generate the second photoelectron.

Direct observation of an EWP in a diatomic molecule is key to exploring coupled nuclear electron motions in more complex molecules. However, the complex molecule will accompany complicated photoelectron spectra, and it will be difficult to elucidate the key electronic states leading to a target chemical reaction. Although attosecond electron motion in molecules can be monitored by detecting ions and photoelectrons in coincidence, the repetition rate of available attosecond light sources is still insufficient to perform attosecond-pump/attosecond-probe measurement. The detection of fragment ions and the identification of the relevant electronic state from nuclear motion by a-few-pulse APT in the present study provide a powerful alternative method for observing attosecond electron motion in complex molecules. The development of wavelength tunable attosecond pulses well matched to the potential energy of the electronic states in molecules can further extend the potential of the proposed scheme for investigating attosecond electron motion and/or coupled nuclear electron motion.

MATERIALS AND METHODS

A-few-pulse APT generation and characterization

The experimental setup for attosecond-pump/attosecond-probe measurement of an EWP in a nitrogen molecule is shown in fig. S1. The experimental setup is composed of three primary components: (i) an intense a-few-pulse APT generator, (ii) a high-throughput, high-stability interferometer with an attosecond time scale, and (iii) a counting velocity map imaging ion spectrometer.

An APT is generated using a sub–15 fs TiS laser system [800 nm, 12 fs, 40 mJ (maximum), 100 Hz] (28). The output of a femtosecond laser system is loosely focused (f = 5 m) onto a static gas cell filled with Xe gas to generate intense high harmonics (29). The resultant harmonic intensity distribution at the focal region is shown in fig. S2 where the throughput of XUV optics [Si plane mirror, SiC concave mirror, XUV
grating, and XUV CCD (charge-coupled device) is taken into account. By tuning the central wavelength of fundamental light, the harmonic distribution is tuned with three configurations. When the central wavelength of fundamental light is in a blue-shift configuration, the resultant harmonic energy is also blue-shifted as shown in fig. S2A. On the other hand, when the central wavelength of fundamental light is in a red-shift configuration, the harmonic distribution is also red-shifted as shown in fig. S2C.

The temporal profile of APT is characterized in situ by measuring an interferometric autocorrelation trace using a nitrogen molecule as a nonlinear medium. By recording the fragment ions originating from two-photon nonsequential dissociative ionization as a function of delay, the interferometric autocorrelation trace is obtained as shown in fig. S3A. The resultant pulse duration of each attosecond pulse is 250 as, and the duration of the APT envelope is 4.2 fs in which the attosecond bursts repeated each half-cycle of the fundamental laser. This short APT envelope suggests that the number of attosecond pulses in the envelope is a few as shown in fig. S3B. Therefore, the generated APT can be referred to as “a-few-pulse APT.” The probability of two-photon processes with a-few-pulse APT is given in fig. S3C. For the purpose of using lower-order harmonics (first through seventh), a thin metal filter, which is usually inserted to block the fundamental light and lower-order harmonics, is not inserted. The unconverted fundamental light is significantly attenuated to avoid multiphoton absorption as described in the following. The resultant pulse duration of a-few-pulse APT is somewhat chirped by the attosecond chirp. The magnitude of the chirp is estimated to be $1.3 \times 10^{-22}$ fs$^2$ (19).

**Excitation with APT**

Molecules pumped with the APT can be excited by multiple attosecond pulses in the train. The effect of an attosecond burst on the VWP is negligible because the envelope of APT (~4 fs) is much shorter than the vibrational period of N$_2$ and N$_2^+$ (14 fs in the shortest). Note that the VWP can only be created when the spectral bandwidth of light source can cover several vibrational states. On the other hand, for observing the EWP, the carrier frequency of light source should be larger than the energy difference of electronic states relevant to the formation of EWP. Our a-few-pulse APT satisfies these conditions. The effect of an attosecond burst on the EWP between the $\tilde{A}^2\Pi_u$ and $C^2\Sigma^+_u$ states is plotted as a function of delay in fig. S4. When the EWP is created by the single pulse excitation, the periodic change of 500 as in the probability of internuclear distance is clearly seen in fig. S4A. On the other hand, when the EWP is created by a-few-pulse APT, the same periodic structure can be observable, although the modulation contrast is lower than the single pulse excitation case shown in fig. S4B.

**High-throughput, high-stability delay line**

The generated intense a-few-pulse APT propagates about 6 m downstream, and the APT passes through a pinhole (2 mmØ). Because the beam diameter of high harmonics is about 3 mmØ, the contribution of the long trajectory is eliminated by the pinhole. At the same time, the significant portion of co-propagated fundamental light is truncated by the pinhole. After passing through the pinhole, the APT pulse is injected into a high-throughput, high-stability interferometer (31). The APT beam is spatially split by a pair of Si plane mirrors. The incident angle for the Si mirror is set to the Brewster angle of the fundamental laser pulse. One of the Si mirrors is mounted on a high-precision piezo linear one-axis translation stage.

The delay between the two replicas of a-few-pulse APT is precisely adjusted by moving the piezo stage. Two types of piezo stages were used for the pump-probe measurement. For measuring the interferometric autocorrelation trace or extracting electronic responses of nitrogen...
molecules, the delay was scanned every 35.6 as from −7 to +7 fs corresponding to moving the piezo stage (P-621.1CL, Physik Instrumente) in 20-nm steps. On the other hand, in measuring the temporal evolution of VWPs, the delay was scanned every 2 fs from 0 to 400 fs corresponding to moving the piezo stage (P-628.1CL, Physik Instrumente) in 1120-nm steps.

The instability of the delay can be suppressed to be smaller than 10 as/hour by actively regulating the temperature of the piezo stage by a Peltier module sandwiched with Cu plates with 0.001°C precision using a high-precision temperature controller (ILX Lightwave, LDT-5910C) because the thermal expansion of the position sensor of the piezo stage decreases the stability of the interferometer. The temperature regulation increases the stability of the interferometer by one order of magnitude. The delay zero is experimentally confirmed by measuring the interferometric autocorrelation trace of the APT.

**Velocity map imaging ion spectrometer**

Replicas of the APT pulses with a fixed delay are propagated to a SiC concave mirror (f = 100 mm) passing through a velocity map imaging spectrometer (VMIS) (32) and are focused onto a molecular beam of nitrogen molecules. The focal intensity is about $1 \times 10^{14}$ W/cm² for both the pump and probe pulses. The molecular beam is injected from a high-speed piezo valve (33) integrated into the rear of a repeller electrode in the VMIS (34). The central part of the molecular beam of nitrogen is skimmed by a pinhole (0.5 mmØ) of the repeller electrode. The density of the molecular beam can be high enough to induce the distortion of the momentum image due to a space charge effect with the intense a-few-pulse APT. In the actual measurement, to avoid image distortion, the sample density is set two orders of magnitude lower than the onset density of the space charge effect.

**Data acquisition conditions and data analysis**

The opening time of the piezo valve can be as short as 20 Data acquisition conditions and data analysis

sample density is set two orders of magnitude lower than the onset den-

sion method (pBASEX) (38).

Here, the temporal evolution of the fragment signal shown in Figs. 2 and 3 is obtained after integration over the angle measured from the laser polarization. The angular distribution of the fragment is used to securely assign the probe processes of each VWP because the angular distribution reflects the symmetry of the electronic states.

**REFERENCES AND NOTES**


**SUPPLEMENTARY MATERIALS**

Supplementary materials for this article are available at http://advances.sciencemag.org/cgi/content/full/1/e1500356/DC1 Experimental setup and conditions

Observation of an electron wavepacket through kinetic energy distribution measurement

Potential energy curves of N₂ and N₂⁺

Vibrational wavepacket

Electron wavepacket

Movie S1. Temporal evolution of the differential EDM.

Fig. S1. Experimental setup.

Fig. S2. Spectrum of fundamental light and high harmonics.

Fig. S3. Interferometric autocorrelation trace of a-few-pulse APT.

Fig. S4. APT pump pulse effect on the interferometric density.

Fig. S5. Potential energy curves of the $\tilde{A}^2\Sigma_g^+$ state and the final states excited from the $\tilde{A}^2\Pi_c$ state.

Fig. S6. Franck-Condon factors of the electronic states in N₂ and N₂⁺.

Fig. S7. Potential energy curves and vibrational distributions of the b$^3\Sigma_u^+$ states.

Fig. S8. Frequency-filtered delay KE spectrogram.

Fig. S9. Numerical simulation of temporal evolution of VWP.

Table S1. Spectroscopic constants of electronic states in N₂ and N₂⁺.

Table S2. Energy of N₂ and N₂⁺ dissociation limits relevant to the probe process of the vibrational and electron wave packet (39).

Table S3. Probe process of vibrational wave packet in X$^2\Sigma_g^-$

Table S4. Probe process of vibrational wave packet in $\tilde{A}^2\Sigma_g^+$

Table S5. Probe process of vibrational wave packet in $\tilde{A}^2\Pi_c$

Table S6. Assignment of observed electron wavepacket at $E = 0.2$ eV.

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58. All data and analysis details presented in this work are available upon request to T.O. or KM.  
59. The authors declare that they have no competing interests. Data and materials availability: All data and  
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