Jamming and overpacking fuzzy microgels: Deformation, interpenetration, and compression

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Tuning the solubility of fuzzy polymer microgels by external triggers, such as temperature or pH, provides a unique mechanism for controlling the porosity and size of colloidal particles on the nanoscale. As a consequence, these smart microgel particles are being considered for applications ranging from viscosity modifiers and sensing to drug delivery and as models for the glass and the jamming transition. Despite their widespread use, little is known about how these soft particles adapt their shape and size under strong mechanical compression. We use a combination of precise labeling protocols and two-color superresolution microscopy to unravel the behavior of tracer microgels inside densely packed soft solids. We find that interpenetration and shape deformation are dominant until, in the highly overpacked state, this mechanism saturates and the only remaining way to further densify the system is by isotropic compression.

INTRODUCTION

Microgels are among the most studied colloidal and polymeric systems of the past two decades (1–4). In particular, microgels made from thermosensitive poly(N-isopropylacrylamide) and its derivatives are of interest (5). By decorating and functionalizing microgels with nanoparticles, one can add additional optical, chemical, or magnetic sensitivity (6–9). Swelling of the microgel by lowering the temperature can drive a colloidal suspension from the liquid to the solid state, conveniently crossing the glass and the jamming transition without the need to prepare samples of varying composition (10–13). In contrast to other soft matter constituents, such as emulsion droplets or bubble foams (14–16), microgels can be highly overpacked, meaning that the effective volume fraction \( \zeta_{\text{eff}} \) can be much larger than one (10, 17, 18). However, little is known about the behavior of the individual microgel particles pack and deform in the jammed and overpacked state, although this will crucially influence the dynamics and macroscopic viscoelastic properties of the amorphous solid (1). Mattsson et al. (17) recently reported that, unlike hard-sphere suspensions, microgels are dynamically arrested and jammed at an effective volume fraction \( \zeta_{\text{eff}} \) much larger than one. At the same time, Zhang et al. (12) reported the jamming of microgels near the expected transition for hard spheres. Much of this marked difference can possibly be explained by the difference in microgel sizes and chemistry, such as the cross-link density, charged groups, and ionic strength. However, direct experimental methods that would allow to clarify the origin of these differences and to characterize the microgels in dense packings in situ are scarce. Although techniques such as atomic force microscopy (AFM) and cryogenic transmission electron microscopy (cryo-TEM) can reach a nanometric resolution, they are limited to surface imaging (AFM) or require harsh sample preparation and offer relatively poor contrast (cryo-TEM) (19). In neutron scattering, averages are taken in reciprocal space over a size distribution of randomly oriented particles, and important information about particle shape anisotropy and particle-particle interpenetration cannot be obtained directly (18). The lack of more detailed information on the single-particle level also limits progress in micromechanical modeling, which until now is often based on simplified assumptions such as Hertzian or harmonic pair-interaction potentials (20, 21), which are not compatible with the highly overpacked states observed in experimental studies. Moreover, packing soft and deformable particles with different shapes, intrinsic or acquired, are interesting motifs not only for microgels but also in many condensed matter systems, with important consequences for the relationship between structure and the attributes of the material building blocks (20, 22).

To understand the microstructural changes at high packing densities, it is important to be aware of the complex architecture of individual colloidal microgel particles. In microgels, the internal cross-link density is not homogeneous, and moreover, microgels have a fuzzy corona with dangling polymer chains (23). The brush-like interactions mediated by these dangling ends can have a profound influence on the onset of repulsive interactions when the microgels swell into contact (11). The low-density polymer corona may also allow for deformation and even some mutual interpenetration between adjacent microgels (24). Thus, the architecture of swollen microgels permits different competing packing mechanisms such as shape deformation, interpenetration, and compression. The main goal of our work is to quantify their relative contribution by nanoscale imaging microgels based on dSTORM (direct stochastic optical reconstruction microscopy) superresolution microscopy (19, 25, 26). To this end, we fluorescently label a small subset of microgels and record ultrahigh-resolution two-dimensional (2D) optical image sections. The combination of precise labeling protocols and superresolution techniques allows us to map out the different contributions from the marginally jammed state to the deeply overpacked regime. STORM is a relatively recent single-molecule localization imaging technique that has gained widespread use in biology, but its applications to soft materials are still rare (19, 25–27). Here, we demonstrate that, when applying precise labeling protocols, STORM can be a unique tool to overcome traditional limitations in optical materials characterization at the submicrometer scale, particularly when taking advantage of the unique specificity of multicolor dye labeling.

RESULTS

Microgel properties

Although the microgels investigated in this study are about 1 μm in diameter, the structural transitions we aim to characterize, as a
We apply dSTORM (Fig. 1. Superresolution microscopy of microgels under dilute conditions. (A) One-color microscopy. From left to right: Wide-field fluorescence image of individual microgels, single-molecule blinking frame, and final dSTORM image reconstructed from 60,000 blinking frames. In red, the smoothed contours correspond to particle sizes of 439 and 424 nm. (B) Two-color microscopy by spectral demixing. Two spatially equivalent but spectrally separated images are captured side by side on the camera, and the intensity ratio between long and short wavelength channels is used to identify different fluorescent dye species. From left to right: Wide-field fluorescence image of two microgels labeled with CF680R (orange) and AF647 (white), single-molecule frame showing different intensity split for the two dyes, and final reconstructed image obtained from single-molecule localizations on each side. Scale bars, 500 nm.

Mean square displacement (μm²)

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<th>Concentration (%)</th>
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<td>7.4</td>
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<tr>
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Fig. 2. MSD for dense microgel suspensions at different concentrations and example tracks (τ ~ 20 s) centered in a circle of the same size as the particles (R = 470 nm). Particles go from simple diffusion at the lowest concentration of 7.4 wt % to complete arrest starting from 8.0 wt %.

function of packing density, occur on a significantly smaller length scale. We apply dSTORM (19, 26, 28) and spectral demixing dSTORM (SD-dSTORM) (29) to achieve nanoscale optical resolution and single-particle specificity. SD-dSTORM is used for two-color imaging, which is necessary to observe interpenetration of particles in contact. We can image individual microgels with a lateral resolution of ≈30 nm as reported in our previous work (26). To this end, we prepare samples at different concentrations, and only a small fraction of fluorescently labeled microgels are included as tracers to achieve optimal contrast. Before imaging, the sample is heated to homogenize it and to erase preparation history and then cooled rapidly to a temperature of 22 ± 1°C. Most of the images we record are 2D projections of a ≈500-nm-thick z-section, which is about half the particle diameter. For one-color imaging, we choose particles located in the bulk of the sample. For two-color dSTORM of adjacent particles, we select pairs of particles in contact with the substrate to ensure that the particle centers of mass are located in the same plane. The quality of the images we obtain is illustrated in Fig. 1 for particles adsorbed on the surface of a glass slide.

We find that the most robust way to determine the size and shape of the microgels is by analyzing the outer contour of a 2D image with an edge detection method and appropriate smoothing filters (see the Supplementary Materials). For isolated microgels, we obtain an effective radius $R = \sqrt{A/\pi} = 429 \pm 9$ nm from area $A$ enclosed by the contour. The edge detection is a trade-off we have to make to be able to capture all the geometrical features of the microgels under dilute and highly packed conditions. When using the edge detection algorithm, we are insensitive to the ultralow-density outer regions of the microgel, and therefore, $R$ is about 10% smaller than the total radius estimated from static light scattering. From the latter, we determine the size of the dense core to $R_{\text{core}} \approx 380$ nm and the thickness of the corona is $2\sigma \approx 90$ nm, giving a total size $R_{\text{tot}} = R_{\text{core}} + 2\sigma = 470$ nm (23, 30). The size polydispersity is approximately 6% (see the Supplementary Materials). To complement our findings in 2D and to demonstrate the potential of dSTORM applied to polymeric soft materials, we also performed a 3D reconstruction of densely packed microgels with an axial resolution of approximately 60 nm (26).

The liquid-to-solid transition

Depending on the polymer weight fraction, the microgel suspension may be quenched in an amorphous liquid or solid state at 22°C. Initially, the repulsive sphere fluid enters the ultrasoft glassy phase at $\xi_\eta \sim 0.58$, and a few percentiles above $\xi_\eta \sim 0.64$, particles touch (21, 31). For hard spheres, this marginal jamming point is also known as random close packing (32). Jamming the soft spheres at densities above $\xi \sim 0.64$ means that the particles have to deform or interpenetrate to fill space more efficiently. We determine the liquid-to-solid transition by video microscopy and particle tracking deep inside the sample (33). Figure 2 shows the microgel’s mean square displacement (MSD) at different concentrations. At the lowest concentration, 7.4 wt % (weight %), the sample is still liquid, exhibiting nearly diffusive behavior with tracks extending beyond the diameter of a particle. Increasing the concentration to 8 wt % changes the behavior completely. The MSD no longer increases linearly in time, as one would expect for a liquid, but exhibits a plateau,
signaling that the sample is a weak solid. Nonetheless, as we can see from the particle track, non-negligible motion is still present, albeit localized, with an average linear displacement of \( \approx 100 \) nm. Further increasing the concentration to 8.9 wt % and then to 10.4 wt % results in displacements of the order of only 15 nm, comparable to the tracking resolution, so that we may consider the particles immobile and begin superresolution imaging.

From the time-resolved measurements of microgel displacements shown in Fig. 2, we determine the jamming point to \( c_J \approx 8 \) wt %, here \( c \) is the mass concentration of the microgel dispersion in wt/wt. From the jamming volume fraction \( \zeta_J \approx 0.64 \), we can determine the swelling ratio \( k \) of our microgels at the selected temperature of \( T = 22 \) \(^\circ\) C. Converting the mass concentration to the effective volume fraction, \( k = \zeta_J/c \approx 8 \) and \( \zeta_{eff} = k c \).

**Global structural evolution of dense microgel assemblies**

We assess the global structural evolution from small-angle light scattering on the same samples used in the dSTORM imaging. The data shown in Fig. 3A show that the microgels pack densely, as highlighted by the pronounced diffraction ring. The absence of Bragg peaks confirms that the microgels are quenched in an amorphous structure and do not crystallize, at least on the time scales of the experiments. The center-to-center pair distance (Fig. 3C) decays as \( c^{-1/3} \), as expected, and the scattering intensities drop almost to zero for \( c > 22 \) wt %, which indicates that the system becomes very homogeneous at high densities. Moreover, we can obtain an estimate of the random close packing threshold by setting the pair distance equal to the unperturbed particle diameter \( 2R = 940 \) nm and find \( c \approx 8 \) wt %, in agreement with the MSD data. In contrast to hard spheres, at this point, the closely packed microgel assembly is still very soft, and the elasticity rises only gradually as the particle volume fraction is increased (10, 11).

**Two-color dSTORM superresolution microscopy of overpacked microgels**

Using dSTORM, we can visualize small-scale size changes and shape deformations that would otherwise be invisible starting from a concentration of 10 wt % to more than \( \approx 30 \) wt % (Fig. 4). At lower concentrations, the microgel is undeformed and begins to be slightly compressed. As the concentration is increased, we begin to see deformations, albeit without significant change in size, and eventually, the microgels become faceted.

![Fig. 3. Small-angle light scattering from dense microgel suspensions.](http://advances.sciencemag.org/)
Fig. 4. One- and two-color superresolution microscopy of densely packed microgels. Wide-field (A) and dSTORM (B) images at high concentration (23.8 wt %). The higher resolution of dSTORM reveals significant microgel deformations. In red, an example of a contour (solid line) and vertices (full circles) used for analysis. (C) 3D dSTORM visualization of microgel particles at high concentration (25.6 wt %). For clarity, the microgel visualizations have been placed closer to each other. An animated 3D rendering is shown in movie S1. (D) dSTORM images of individual microgels showing compression and deformation as the concentration is increased. (E) Two-color 2D dSTORM of microgel pairs revealing partial interpenetration besides compression and deformation. Contour lines are shown for the 23.8 wt % sample with a relative overlap area of 17.38%. Scale bars, 500 nm.

at 16.4 wt % (Fig. 4, B and D). In Fig. 4C, we show a 3D reconstruction of several microgel particles at 25.6 wt % located in the vicinity of the glass interface. Although the z-resolution in 3D dSTORM (26) is a bit lower, we can still observe the irregular shape and faceting of the microgels. From the 2D two-color images (Fig. 4D), we observe that the microgels interpenetrate, and the overlap area increases in this regime (24, 34). Once the ability to deform the particles is exhausted, only compression remains as a means to accommodate higher polymer concentrations. Above 22 wt %, we observe a steady decrease in particle size and no further increase in particle overlap.

The shape of highly deformed incompressible soft spheres, such as dense emulsions with a filling fraction approaching unity, is similar to the faceted polyhedral shape of air bubbles in dry foams (35, 36). The 3D reconstruction (Fig. 4C) indicates a polyhedral shape. However, extracting a full set of quantitative 3D data is very demanding (26), and moreover, the quality of the data is adversely affected by the lower axial resolution. A full 3D study is therefore beyond the scope of this work. Conversely, we extract information about the packing and deformation of microgels by analyzing the contour of 2D images of each microgel. To quantify the shape changes of the microgel particles, we calculate the isoperimetric quotient IsoQ = 4πA/P², where A denotes the enclosed surface and P denotes the perimeter. A perfect circle has IsoQ = 1, whereas polygons have lower values; for example, a regular hexagon has IsoQ ≈ 0.91. We measure interpenetration from the overlap area between two microgels, with areas A₁ and A₂, as A₀ = 2A₁A₂/(A₁ + A₂), as shown in Fig. 5. The particle effective radius is R = √A/π. In addition, we identify the vertices of the particles as the local maxima of curvature of the contour (Fig. 4B). The number of facets n is then equal to the number of vertices.

**DISCUSSION**

On the basis of the experimental data (Fig. 5), we can identify the three consecutive stages in the packing process. In the first stage, no deformation of the particle contour can be detected, with values of IsoQ compatible with those in dilute conditions. Microgels are mildly compressed, but their shape is visually unchanged. Notice that this does not exclude the weak deformation of the outer particle corona, which is
MATERIALS AND METHODS

Synthesis and characterization

Microgels were synthesized by free radical precipitation polymerization to obtain micrometer-sized particles as described in previous studies (10, 26). N-isopropylacrylamide (NIPAM) was used as the monomeric unit, N,N'-methylenebisacrylamide (BIS) was used as cross-linker, and 2,2'-azobis(2-methylpropionamidine) dihydrochloride was used as initiator. To allow for fluorescent labeling with different dyes, free amines were introduced via a co-monomer, N-(3-aminopropyl)methacrylamide hydrochloride (APMA). Any dye that is amine-reactive, such as the N-hydroxysuccinimide (NHS) ester varieties, can be added at a later time. The result is microgels with a cross-linking of 4.9 mol % (mole percent) and co-monomer concentration of 0.27 mol %. The greatest effects that we aim to characterize occur at the periphery of the microgel, where the polymer density is significantly lower than in the core. To achieve better contrast when imaging, it is thus preferable to predominantly label the outer region of the microgels. To this end, the co-monomer was added continuously to the solution starting 10 min after particles have begun nucleating, which was signaled by the solution going from transparent to milky white. Dense samples were obtained by centrifugation of a dilute stock suspension and removal of the supernatant. The final concentration was determined by drying and weighing.

One- and two-color superresolution microscopy

For one-color imaging, we labeled microgels with the fluorophore Alexa Fluor 647 (AF647). To achieve blinking of fluorophores, we added 50 mM cysteamine (Sigma-Aldrich) and adjusted the pH to 8 using HCl (26). For two-color dSTORM, the cysteamine concentration was increased to 100 mM. First, a conventional wide-field image was taken for reference, and then the laser illumination power was increased to reach stochastic blinking conditions of the fluorophores (25). Between 60 and 80,000 frames were then recorded at 60 to 100 frames beyond the detection limit of dSTORM. At the same time, we observe the onset of interpenetration (34). In the second stage, above $c \sim 15$ wt% ($\zeta_{\text{eff}} \sim 1.3$), the pair distance falls below the size of the particle core $2R_{\text{core}} \approx 760$ nm. Now, the most marked feature we observe is the steady decrease of IsoQ, meaning that microgels are deforming, as can be seen by the unaided eye in the dSTORM images (Fig. 4). A maximum of deformation is asymptotically reached, and IsoQ plateaus at $\approx 0.975$. For these highly deformed particles ($c \geq 23.8$ wt%), we find that the mean number of facets is $n \sim 6$, with no measurable dependence on concentration (see also the Supplementary Materials). Overall, the IsoQ value is still quite large as compared to the hexagon value, which can be explained by the projection of the 3D shape to the imaging plane, the smooth contour, and rounded corners we obtain even for the most deformed microgels. Nonetheless, the imaging data capture well the onset and saturation of deformation. In parallel, interpenetration continues because the formation of facets increases the contact area. Between 15 and 22 wt%, the particle volume remains almost constant. Once the shape deformation is complete, the final stage is reached. Now, the volume is filled almost homogeneously by the polymer gel. The latter is also confirmed by the vanishing light-scattering contrast (Fig. 3). For $c > 22$ wt% ($\zeta_{\text{eff}} \sim 1.75$), the microgels are highly overpacked and both interpenetration and deformation saturate, leaving compression as the only possible mechanism for accommodating higher polymer concentrations up to the highest densities studied ($\zeta_{\text{eff}} \gtrsim 3$). For $\zeta_{\text{eff}} \gtrsim 1.75$, we observe a continuous decrease of the particle radius $R \sim c^{-1/3} \sim \zeta_{\text{eff}}^{-1/3}$, which is a consequence of adding more particles to the same total volume of the container.

Fig. 5. Mechanisms involved in densely packed colloidal sized fuzzy microgels. (A) Reduction of effective radii. (B) Isoperimetric quotient. Horizontal dotted line is the measured value under dilute conditions. Each point is obtained from 30 to 50 microgels. (C) Increased overlap area as a function of concentration. Each point corresponds to a single pair. Vertical dashed lines separate the different compression-deformation stages identified in this work. (I) Weak compression and onset of interpenetration. (II) Shape deformation and interpenetration. (III) Isotropic compression of the microgel particles. The effective volume fraction $\zeta_{\text{eff}}$ is related to the mass concentration $c$ via the swelling ratio $k \sim 8$, $\zeta_{\text{eff}} = k c$. 

per second. The acquisition of a superresolution image requires that the sample remains immobile for the duration of the experiment, which is typically several minutes. We found that only sufficiently elastic samples, \( c > 10\% \), can be studied with dSTORM. Single fluorophores were localized, and the coordinates were used to reconstruct a superresolved image (37, 38). 3D imaging was performed using the method of astigmatism (39), which we implemented using the adaptive optics microscope add-on MicAO (Imagine Optic), as described previously (26).

For the two-color dSTORM, we labeled tracer microgel particles with two different dyes and then imaged them separately. For the implementation of this two-color superresolution microscopy, we added a second dye, CF680R, which performed comparably to AF647 under the same conditions (40). Utilizing two dyes with partially overlapping absorption and emission spectra, allowed us to excite both dyes with a single laser with \( \lambda = 639\) nm. The emitted light was then split via a dichroic mirror with a cutoff wavelength of 690 nm, and two spectrally distinct images, covering the same field of view, were formed side by side on the camera. The cutoff wavelength was chosen such that single-fluorophore images appear on both sides but with their intensity split differently depending on the fluorophore. Using freely available software (41), we found pairs of localizations and measured the ratio of intensities between the two. On the basis of previous calibration measurements performed with the two fluorophores, we could determine which type of fluorophore had produced a given intensity ratio and assign a color (details in the Supplementary Materials). Using this method, we achieved a color cross-talk of only 1%. The final superresolution image was reconstructed with localizations obtained from only one side, thereby avoiding further registration errors. Imaging conditions were the same as for one-color imaging. As an example, we imaged (Fig. 1B, conventional and SD-dSTORM) a mixture of microgels labeled with AF647 and CF680R. The same quality and level of detail were achieved for both colors. Two-color images of microgel pairs were taken at the surface only. This choice was made to ensure that the two microgels were at the same height, thus limiting projection artefacts when quantifying the data for interpenetration.

**Image analysis**

We used a two-step method implemented in Matlab to delineate the microgel contour. First, the rough contour was determined using a Laplacian of Gaussian edge detection method. Second, we smoothed the contour using Fourier descriptors (42). The method works by mapping the boundary coordinates onto complex numbers \( z = x + iy \), followed by taking the Fourier transform. An inverse transform would yield the original shape, whereas using just a few terms, or descriptors, out of over 100 before back-transforming effectively removes high-frequency noise. Using this method, we sacrificed sharp corners but gained a more reliable measure of perimeters (see also the Supplementary Materials). From the smoothed contour, we obtained the area and the perimeter \( P \) that we used to calculate an effective radius \( R = \sqrt{A/P} \).

We measured the curvature \( \kappa \) along the contour \( r = (x, y) \) in Cartesian coordinates, defined as \( \kappa = |x'y'' - y'x''|/(x'^2 + y'^2)^{3/2} \). We then identified the vertices of the particles as the local maxima of curvature (Fig. 4B). The number of facets \( n \) was equal to the number of vertices.

**Small-angle light scattering**

A collimated laser beam with \( \lambda = 532\) nm impinges on a thin layer of compressed microgels, sandwiched between a glass coverslip and cover slide, with a thickness of \( h \sim 50 \text{ to } 100\ \mu m \). Diffracted light was collected on a screen placed at a distance \( D \) away from the sample, which was then imaged with a camera. Every point on the screen, with distance \( r \) from the optical axis, defines an angle \( \tan(\theta) = r/D \) and a scattering vector \( q \) with magnitude \( q = 4\pi/\lambda \sin(\theta/2) \). The peak in diffraction is related to the particle’s center-to-center pair distance through \( d \sim 2\pi/\max(q) \).

**Supplementary Materials**

Supplemental material for this article is available at http://advances.sciencemag.org/cgi/content/full/3/10/e1700969/DC1

section 51. Static light scattering characterization

section 52. Contour of microgel images

section 53. Two-color superresolution microscopy—Calibration procedure

fig. 51. Form factor of pNIPAM microgels in dilute conditions.

fig. 52. Determination of microgel contours by using Fourier descriptors.

fig. 53. Assessment of correlations between size and shape.

fig. 54. Sample images of deformed microgels at 34 wt % with different values of \( I_0/Q \).

fig. 55. Vertices detected as maxima of curvature for deformed particles at different concentrations.

fig. 56. Distribution \( \max(I_{\text{max}})/I_0 \) at a concentration of 23.8 wt %.

fig. 57. Principle of two-color imaging by spectral demixing.

**References and Notes**


