K-Λ crossover transition in the conduction band of monolayer MoS$_2$ under hydrostatic pressure

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Monolayer MoS$_2$ is a promising material for optoelectronics applications owing to its direct bandgap, enhanced Coulomb interaction, strong spin-orbit coupling, unique valley pseudospin degree of freedom, etc. It can also be implemented for novel spintronics and valleytronics devices at atomic scale. The band structure of monolayer MoS$_2$ is well known to have a direct gap at K (K' point), whereas the second lowest conduction band minimum is located at Λ point, which may interact with the valence band maximum at Κ point, to make an indirect optical bandgap transition. We experimentally demonstrate the direct-to-indirect bandgap transition by measuring the photoluminescence spectra of monolayer MoS$_2$ under hydrostatic pressure at room temperature. With increasing pressure, the direct transition shifts at a rate of 49.4 meV/GPa, whereas the indirect transition shifts at a rate of −15.3 meV/GPa. We experimentally extract the critical transition point at the pressure of 1.9 GPa, in agreement with first-principles calculations. Combining our experimental observation with first-principles calculations, we confirm that this transition is caused by the K-Λ crossover in the conduction band.

INTRODUCTION

Atomically thin transition metal dichalcogenides (TMDCs) have attracted great attention during the past few years, among which monolayer MoS$_2$ [a two-dimensional (2D) direct bandgap semiconductor] has been in the spotlight of 2D material research. Monolayer MoS$_2$ exhibits a sandwich structure with a plane of Mo atoms covalently bonded to two planes of sulfur atoms, as shown in Fig. 1A. Although multilayer and bulk MoS$_2$ have an indirect bandgap between Λ point in the conduction band and Γ point in the valence band due to strong coupling of p orbits of the sulfur atoms between the layers, in contrast, the monolayer MoS$_2$ has a direct bandgap in the visible regime (1, 2), which is ideal for the exploration of optoelectronic applications. Its conduction band minimum (CBM) and valence band maximum (VBM), dominated by d orbits of Mo atoms (3), are located at the doubly degenerate corners (K and K') of the hexagonal Brillouin zone. The second lowest CBM at Λ point and the second highest VBM at Γ point, as shown in Fig. 1A, are dominated by both d orbits of Mo atoms and p orbits of S atoms. The different pseudospin configurations for excitons at K and K' valleys in monolayer MoS$_2$ (4) bring about an optical selection rule (5–8), in which the two valley states couple respectively to a $\sigma^+$ or $\sigma^-$ circularly polarized photon only, as well as other novel phenomena, such as the valley Hall effect (4, 9). Combining with its other unique and appealing features, such as an exceptionally large Coulomb interaction (10–13) and strong spin-orbit coupling (14–16), monolayer MoS$_2$ becomes a promising material for applications in optoelectronics, spintronics, and valleytronics (17–19).

Atomically thin TMDCs are also promising candidates for nanoflexible devices. Compared with bulk materials, strain will be much easier to apply in these 2D materials and will cause many effects in the applications. Applying strain and stress is a proven strategy for modulating the band structure of semiconductors (3, 20–29), especially for semiconductors with multivalleys in the Brillouin zone. Because of different shift rates of various valleys with increasing pressure, the bandgap may change from direct to indirect or vice versa. For monolayer MoS$_2$, the valley effects mainly exist in the direct K-K transition; thus, it is important to clarify the relationship of the band structure versus pressure for strain-based applications. Theoretical calculations for monolayer MoS$_2$ result in direct-to-indirect bandgap transition under both tensile (3, 25, 30) and compressive strains (3, 25, 27, 31) with different mechanisms. Here, tensile and compressive strain means the crystal lattice that is being enlarged or reduced, respectively. The former is thought to be caused by the transition of the VBM from K to Γ valley (3, 25, 30), whereas the latter is still controversial, because it could be due to the change of either CBM from K to Λ valley (3, 25, 30, 31) or VBM from K to Γ valley (27). Referring to the aspect of experiments, although many studies (26–28, 32, 33) have been performed, the transition is not really seen under tensile strain, whereas it is still absent under compressive strain.

Applying hydrostatic pressure by DAC has been proven an effective approach for tuning and probing the electronic structure of semiconductors. It could vary the lattice constant and tilt the angle between the strong Mo-S bonds of monolayer MoS$_2$, thus altering the interaction strength between different electronic states and deforming the band structure continuously and controllably. Combining it with photoluminescence (PL) spectroscopy, which directly probes the energy of the electron–hole pairs (or excitons), one can unambiguously determine the energy shift of the electronic bands at various locations in the reciprocal space, thus demonstrating the band structure evolution by hydrostatic pressure modulating.

Here, the experimental evidence for direct-to-indirect bandgap transition of monolayer MoS$_2$ is observed by PL spectra under hydrostatic pressure at room temperature. With increasing pressure, the energy peak first exhibits a blue shift at a rate of 49.4 meV/GPa and then a red shift at a rate of 15.3 meV/GPa. The critical turning pressure

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occurs at 1.9 GPa. Combining with first-principles calculations, we can confirm that this transition comes from the change of the CBM from K to L valley. In addition, the energy difference at atmosphere between the K and L valleys in the conduction band is derived to be 118 meV.

**RESULTS AND DISCUSSION**

The as-grown MoS₂ sample is monolayer and uniform, which was characterized by optical microscope, atomic force microscope (AFM), and Raman spectrum, as shown in Fig. 1 (B and C). The PL was collected with a micro-PL system with pressure applied by a DAC device, as schematically shown in Fig. 1D. The PL spectra of the monolayer MoS₂ at various pressures are shown in Fig. 2A, with background signal subtracted. Here, the pressure is isotropic for the monolayer MoS₂. The Si substrate (with a layer of 300-nm SiO₂ on its surface) does not transmit an additional pressure in plane, as proved by the Raman spectra (fig. S1) shown in the Supplementary Materials. For the initial pressure at 0.9 GPa (below that pressure, the pressure calibration was not accurate), the PL peak at 1.82 eV corresponds mainly to the direct K-K transition due to its direct transition nature. The PL curves at different pressures were fitted using Lorentz function to obtain the major peak position under different pressures, as shown by black square dots in Fig. 2B. With increasing pressure, the peak energy first blue shifts and then red shifts, where a clear pressure-induced changeover of the optical bandgap occurs at approximately 1.9 GPa, indicating a direct-indirect bandgap transition.

The turnover from blue shift to red shift of the PL peak energy can be well understood, considering the effect of anticrossing of the electronic states under pressure. Pressure-induced band anticrossing behaviors have been found in III-V and II-VI semiconductors (34–39). We consider this mechanism for the analysis and take the predominant peak as the lower branch. The upper branch is hard to clarify accurately because of the large full width at half maximum at room temperature.

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**Fig. 1. Sample and technical information.** (A) Schematic diagram of the lattice structure and band structure of monolayer MoS₂, where a represents the in-plane lattice constants. (B) The left image is the surface morphology of the as-grown sample under optical microscope. The green area is monolayer MoS₂, and pink area is the Si/SiO₂ substrate without MoS₂. The right image is the AFM image of the as-grown sample, showing that the MoS₂ is monolayer. (C) Raman spectra of the as-grown sample. (D) Schematic diagram of the diamond anvil cell (DAC) used for applying hydrostatic pressure to the sample.

**Fig. 2. Pressure-dependent PL spectra of monolayer MoS₂.** (A) PL spectra of monolayer MoS₂ for various pressures, with background signal subtracted. (B) The evolution of energy of the predominant PL peak versus pressure. Black dots represent peak energies of monolayer MoS₂ under various pressures, taken as the lower branch; red solid line represents the fitting result of the lower branch; and black and red dotted lines represent the direct and indirect transition under various pressures extracted from the fitting, respectively. (C) Integrated intensities of PL peak under various pressures.
It is assumed that the relationship between the direct K-K transition energy and pressure obeys an equation of $E_{1}(p) = E_{10} + k_{1}p$, where $E_{1}(p)$ represents the energy of K-K transition, $E_{10}$ represents the original bandgap of the K-K transition, $k_{1}$ is the pressure rate of the transition, and $p$ is the pressure. While the relationship between the indirect transition energy and pressure obeys a similar equation of $E_{2}(p) = E_{20} + k_{2}p$, the anticrossing-resulted lower branch was fitted by using the following formula, taking the lower value of the equation

$$E_{\pm} = \frac{[E_{10} + E_{20} + (k_{1} + k_{2})p] \pm \sqrt{(E_{10} - E_{20} + (k_{1} - k_{2})p)^2 + 4\lambda^2}}{2}$$

where $\lambda$ is an interaction parameter. Here, we neglect the exciton binding energy, because it is usually considered not to be affected by pressure (32, 40, 41). The result is shown as the red solid line in Fig. 2B. Through the fitting, we obtained that the energy difference at atmosphere between the K and L valleys in the conduction band is 118 meV, whereas the pressure coefficients are 49.4 and $-15.3 \text{ meV/GPa}$ for the direct and indirect transitions, respectively.

The integrated intensity of the PL peak under various pressures is shown in Fig. 2C. One can see that the intensity continuously decreases with pressure. This is related to electrons transferring from K to its adjacent valley in the conduction band or valence band, because the band structure gradually changes from direct to indirect with increasing pressure. Moreover, the slopes change at around 1.8 GPa, indicating a transition of the recombination nature from direct to indirect occurring at this pressure. It is found that the intensity shows a discontinuity at the transition point. We believe that there exists a competition between the direct and indirect transition around the crossing-over point, where they have the same transition energy. The interference between them along with the anticrossing effect results in a reduction in transition probability of both transitions.

**THEORETICAL CALCULATIONS**

First-principles calculations are carried out to simulate the band evolution under various pressures. The relationships of direct (K-K) and indirect (L-K and K-\Gamma) bandgap versus pressure are shown in Fig. 3. The monolayer MoS$_2$ at atmosphere is a direct bandgap semiconductor, with both CBM and VBM located at K point, as shown in Fig. 3A. As the applied pressure increases, the K valley of the conduction band goes upward, whereas A valley goes downward, resulting in a crossover of two valleys at 2.1 GPa, as shown in Fig. 3B. For pressure above 2.1 GPa, the A valley of the conduction band becomes lower than the K valley, as shown in Fig. 3C, resulting in an indirect bandgap. For the relationship of bandgap evolution versus pressure, Fig. 3D shows that with pressure increasing, the direct K-K gap decreases, whereas the indirect L-K gap decreases, and the crossover point is 2.1 GPa, consistent with our experimental results. Besides, the gap between CBM at K point and VBM at \Gamma point is enlarged; thus, the possibility of K-\Gamma crossover in the valence band is excluded in the interpretation of the experimental results. This can be physically attributed to the increasing internal angle of the S–Mo–S bond under pressure (31). The states at the bottom of the conduction band at A point (BCB-A) and that at the top of the valence band at K point (TVB-K) make a pair of bonding and antibonding states with mainly $d_{xz}$ and $d_{yz}$ characters, whereas the states at BCB-K and that at TVB-\Gamma make a pair of states with mainly $d_{z^2}$ character. When the bond angle

![Fig. 3. First-principles calculations for the relationship of bandgap versus pressure. (A to C) are calculated band structures at 0, 2.1, and 2.5 GPa, respectively. The VBM of K point is set to be zero. (D) Functional relationships of bandgap versus pressure. Black, red, and blue dots represent the \Lambda-K, K-K, and K-\Gamma transitions, respectively.](http://advances.sciencemag.org/)
increases because of applied pressure, the coupling between BCB-K and TVB-Γ strengthens, whereas that between BCB-A and TVB-K weakens. Thus, the energy splitting of the pair of states at BCB-K and TVB-Γ increases, whereas that at BCB-A and TVB-K decreases with increasing pressure. This finally results in the K-A crossover in the conduction band. Thus, it is confirmed that the transition that occurred in our experiments is truly due to the change of the CBM from K to A valley.

**SUMMARY**

In summary, by using hydrostatic pressure PL measurements, we experimentally demonstrate the K-A crossover in the conduction band in monolayer MoS2, in agreement with theoretical calculations. With increasing pressure, the predominant PL peak exhibits first a blue shift at a rate of 49.4 meV/GPa and then a red shift at a rate of 15.3 meV/GPa, with a crossing point at 1.9 GPa, indicating a direct-indirect transition of band structure at that critical pressure. The integrated intensity of the PL peak decreases with increasing pressure at different rates, with a turning point at around 1.8 GPa, further evidencing our observation of the critical point of transition. In addition, first-principles calculations are carried out to simulate the band structure of monolayer MoS2 at different pressures, resulting in a K-A crossover in the conduction band occurring with increasing pressure, with the turning point at 2.1 GPa, consistent with our experimental observation. We therefore conclude that the direct-indirect bandgap transition under hydrostatic pressure originates from the K-A crossover in the conduction band of monolayer MoS2.

Different from the direct-to-indirect transition from monolayer to multilayer TMDCs (mainly caused by increasing interlayer coupling), the transition occurring under pressure for monolayer MoS2 is caused by the pressure-induced K-A crossover transition in the conduction band. Because of the lack of interlayer coupling in monolayer MoS2, this transition mechanism is an intrinsic intralayer nature, which is only related to the interaction of atoms within a monolayer. Moreover, this conclusion may be extended to other semiconductors, especially those with multivalleys in the Brillouin zone, such as other monolayer TMDs (WS2, MoTe2, etc.), owing the same crystal structure and similar band structure with monolayer MoS2.

**MATERIALS AND METHODS**

**Sample fabrication**

Monolayer MoS2 was grown by a chemical vapor deposition method in a dual-temperature zone system using S (99.999%; Ourchem) and MoO3 (99.99%; Ourchem) as sources, perylene-3,4,9,10-tetracarboxylic acid tetrapotassium salt as a seeding promoter, pieces of prethinned Si substrate with a layer of 300-nm SiO2 on its surface as substrates, and high-purity inert argon as carrier gas. The layer number of the as-grown MoS2 was identified by optical microscope and micro-Raman measurement.

**Experimental setup**

Micro-PL measurements were carried out at room temperature with a microscope imaging system. A continuous-wave laser with wavelength of 532 nm and stable power of 10 mW was focused on the sample in a DAC device by a long working distance objective (50x; numerical aperture, 0.35), and the focus spot size was about 7 μm. In the experiment, the laser power below 18 mW is safe for the sample. The PL signal from the sample was collected by the same objective and then sent to a HORIBA iHR550 spectrometer, where the final detection was carried out by a liquid nitrogen–cooled charge-coupled device. The data acquisition time of the PL measurements is 1 s. The pressure was applied by a DAC device with 300-μm diameter of culets. Silicon oil was used as the pressure-transmitting medium, and the pressure was determined by the shift of the R1 fluorescence line of ruby at alongside of the sample.

**First-principles calculations**

Our first-principles calculations were performed by using density functional theory in the generalized gradient approximation with Perdew-Burke-Ernzerhof functional for electron exchange and correlation potentials, as implemented in the Vienna Ab initio Simulation Package (42–44). The 4p, 4d, and 5s electrons of Mo atom and 3s and 3p electrons of S atom were treated as the valence electrons. The electron-ion interaction was described by using the projector augmented-wave method, and the energy cutoff was set to 500 eV. The structures were fully optimized by using the conjugate gradient algorithm until the maximum energy difference and residual atomic forces converge to 10–4 eV and 0.01 eV/Å, respectively. A well-converged Monkhorst-Pack k-point set of 21 × 21 × 1 was adopted, and a vacuum layer larger than 20 Å was used to ensure the decoupling between the periodically repeated cells. The spin-orbit interaction was included in our calculations.

**SOFTWARE AND HARDWARE**

The calculations were performed on a Windows 8.1 computer with an Intel Xeon processor. The Vienna Ab initio Simulation Package was used for all calculations. The Monkhorst-Pack k-point set and the vacuum layer were set as 21 × 21 × 1 and 20 Å, respectively. The energy cutoff was set to 500 eV.

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**REFERENCES AND NOTES**


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**SUPPLEMENTARY MATERIALS**

Supplementary material for this article is available at http://advances.sciencemag.org/cgi/content/full/3/11/e1700162/DC1

fig. S1. Raman spectra of monolayer MoS2 under various pressures. References (45, 46).

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