Experimental evidence of hourglass fermion in the candidate nonsymmorphic topological insulator KHgSb

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Topological insulators (TIs) host novel states of quantum matter characterized by nontrivial conducting boundary states connecting valence and conduction bulk bands. All TIs discovered experimentally so far rely on either time-reversal or mirror crystal symmorphic symmetry to protect massless Dirac-like boundary states. Several materials were recently proposed to be TIs with nonsymmorphic symmetry, where a glide mirror protects exotic surface fermions with hourglass-shaped dispersion. However, an experimental confirmation of this new fermion is missing. Using angle-resolved photoemission spectroscopy, we provide experimental evidence of hourglass fermions on the (010) surface of crystalline KHgSb, whereas the (001) surface has no boundary state, in agreement with first-principles calculations. Our study will stimulate further research activities of topological properties of nonsymmorphic materials.

INTRODUCTION

The discovery of symmetry-protected states of matter in time-reversal topological insulators (TIs) and topological semimetals (1–9) has attracted tremendous interest in a wide range of areas from condensed matter physics to materials science and high-energy physics. The first discovered TI (10) has time-reversal symmetry with Kramers degeneracy protecting nontrivial conducting states on the boundary. Over the past decade, the classification of topological insulating phases has been theoretically extended to many other discrete symmetry classes (11–18). Among these, we mention particle-hole symmetry for topological superconductors, certain magnetic translation symmetry for antiferromagnetic TIs, and crystal symmetries for topological crystalline insulators (TCIs). TCIs studied in the past rely on the presence of a symmorphic mirror plane. In all the previously known cases, time-reversal and/or crystal symmetry generically protects massless boundary states with the usual Dirac-like dispersion (10, 19). Among spatial symmetries, symmorphic symmetries preserve the origin, whereas nonsymmorphic symmetries unavoidably translate the origin by a rational fraction of the lattice vector. The fractional translation could, in principle, play an important role in the classification of band topologies without analog in symmorphic crystals (20, 21). Very recently, Wang et al. (22) and Alexandradinata et al. (23) proposed the first theory of nonsymmorphic time-reversal–invariant insulators. In contrast to the surface Dirac fermions ubiquitous in symmorphic TIs, nonsymmorphic TIs exhibit exotic surface fermions with hourglass-shaped dispersion (Fig. 1A). Wang et al. (22) also proposed that this new kind of TI can be realized in the series of three materials KHgX (X = As, Sb, and Bi).

We start with a brief review of the surface state properties predicted theoretically for KhgSb, which is measured experimentally here. KhgSb has a layered crystal structure constructed from alternately stacked honeycomb HgSb and trigonal K layers. Previous ab initio calculations have predicted that the single-layered KHgSb is a weak TI, whereas the double-layered KHgSb is a trivial insulator, in which only time-reversal symmetry was considered (24). The double-layered KHgSb has a nonsymmetric space group $P6_3/mmc$ (SG 194) generated by screw rotation and glide mirror symmetries. Wang et al. (22) pointed out that the glide reflection $M_x$, indicated as yellow plane in Fig. 1B, is crucial to form the hourglass fermions on the (010) surface. As illustrated in Fig. 1E, because of time-reversal symmetry, the complex-conjugate $M_x$ eigenvalues are paired at time-reversal–invariant momenta $\Gamma$ and $\bar{Z}$ as $\pm i$ and $\pm 1$ (or $-1$) pairs, respectively. The degeneracies at $\Gamma$ and $Z$ have to exchange glide partners along the glide-symmetric line $\Gamma - \bar{Z}$, resulting in an hourglass-shaped dispersion along $\Gamma - \bar{Z}$. The crossing of the hourglass is stabilized by glide symmetry.

RESULTS

The chemical composition of KHgSb single crystals is confirmed by core-level photoemission measurements. As shown in Fig. 1G, the characteristic peaks of K, Hg, and Sb elements are observed. Because the theoretical prediction relies heavily on the nonsymmetric crystal structure, we have performed x-ray diffraction (XRD) measurements on both single crystal and powder of KHgSb. On the basis of the XRD data, we determine that KHgSb has a nonsymmetric double-layered structure with space group $P6_3/mmc$ or $P6_3mc$ (SG 186) (see the Supplementary Materials for details on structural analysis). Because both variants have the same nontrivial topology defined by the glide symmetry $M_x$, our discussion will be limited to space group $P6_3/mmc$, which has been assumed in the theoretical work of Wang et al. (22). The XRD data on the (001) plane of KHgSb single crystal exhibit sharp (001) diffraction peaks (Fig. 1F), indicating that the samples are well crystallized. The low-energy electron diffraction (LEED) pattern on the (001) surface shows a hexagonal structure, consistent with the sixfold symmetry of the crystal structure (Fig. 1F, inset).

To search for hourglass fermions, we performed systematic angle-resolved photoemission spectroscopy (ARPES) measurements to...
Fig. 1. Hourglass fermions predicted in KHgSb with nonsymmorphic spatial symmetry. (A) Schematic surface state bands for materials with symmorphic and nonsymmorphic spatial symmetries. Panels (i) and (ii) present topologically trivial and nontrivial cases with symmorphic spatial symmetry, respectively. Panels (iii) and (iv) are the same as (i) and (ii), respectively, but with nonsymmorphic spatial symmetry showing hourglass-shaped surface band dispersion. (B) Crystal structure of double-layered KHgSb with space group P6/mmc (no. 194). The yellow plane indicates the glide mirror plane \( \overline{M} \), preserved on the (010) side surface. The arrows and coordinates indicate the operation of the glide reflection \( \overline{M} \). (C) Three-dimensional (3D) bulk BZ of KHgSb as well as its projected (001) and (010) surface BZs. (D and E) Projections of calculated bulk and surface bands on the (001) and (010) surfaces of KHgSb, respectively. The calculations show hourglass-shaped surface bands along the glide-symmetric line \( \overline{M} - Z \) on the (010) surface. The complex-conjugate \( M \) eigenvalues are paired as \( \pm i \) pairs at \( \overline{\Gamma} \) and \( +1 \) (or \( -1 \)) pairs at \( Z \). (F) Logarithmic plot of XRD data measured on the (001) plane of KHgSb single crystal. The peaks marked by stars are from the Sb flux. Inset: LEED pattern shows the hexagonal structure of the (001) surface. arb.u., arbitrary units. (G) Core-level photoemission spectrum showing characteristic peaks of K 3\( p \), Hg 5d, and Sb 4d core levels.

Fig. 2. Electronic structure on the KHgSb (001) surface. (A) 3D intensity plot of ARPES spectra showing the electronic structure of valence bands in the \( k_x k_y \) plane. (B) ARPES intensity plot along \( \overline{\Gamma} - M - K - \overline{\Gamma} \) after in situ K doping, showing the bottom of the conduction bands. (C) ARPES intensity plot showing band dispersions along \( \overline{\Gamma} - M - K - \overline{\Gamma} \) on the pristine (001) surface. The dashed curves represent the calculated bulk bands at \( k_z = 0 \). Because generalized gradient approximation (GGA) calculations usually underestimate the bandgap of semiconductors, we rigidly shifted the calculated conduction bands upward to have a 0.46-eV bandgap, which is the value determined experimentally in (B). For clarity, the chemical potential of the calculated band structure is chosen to have the best match with the measured valence band dispersions. (D) Corresponding curvature intensity plot of (C).
investigate the electronic structure of KHgSb. We first summarize the ARPES results recorded on the (001) surface of KHgSb in Fig. 2. The chemical potential on the pristine surface lies in the bandgap between the valence and conduction bands (Fig. 2, C and D), demonstrating the insulating nature of the bulk states in this material. The measured band dispersions along the high-symmetry lines $\Gamma - M - K - \bar{\Gamma}$ are in good agreement with the calculated valence band structure (Fig. 2, C and D). The valence bands form an "M"-like top along both $\Gamma - M$ and $\Gamma - K$. The band top is close to Fermi energy ($E_F$), resulting in enhanced spectral intensity in the vicinity of $\Gamma$ at $E_F$ in Fig. 2A.

To observe the conduction bands, we deposited potassium atoms onto the (001) surface in situ, which dopes electrons into the surface layer and thus shifts the local chemical potential upward. The bottom of the conduction bands is observed around $\Gamma$ after deposition of potassium (Fig. 2B). No sign of surface state is observed within the bulk bandgap, in agreement with the theoretical prediction.

We then turn our focus to the ARPES results recorded on the (010) surface, where the hourglass-shaped surface state was predicted to exist. As illustrated in the top-down view of the lattice in Fig. 2B of Wang et al. (22), the crystal structure of KHgSb can also be described as a stacking of chemically equivalent monatomic layers along the (010) direction, but the interlayer coupling along (010) is much stronger than that along (001). Thus, it is more difficult to obtain a flat (010) surface by cleaving. After many attempts of in situ cleaving, we succeeded in obtaining a mirror-like (010) surface several times. Highly dispersive and well-defined bands are observed with good reproducibility. We performed

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**Fig. 3. Band dispersions along $\Gamma - \bar{\chi}$ on the KHgSb (010) surface.** (A) ARPES intensity plot at $E_F$ recorded along $\Gamma - \bar{\chi}$ by varying the photon energy from 20 to 100 eV on the (010) surface, which maps the $k_x$-$k_y$ plane at $k_z = 0$ of the 3D bulk BZ. The overlaid hexagons indicate the BZ structure in the $k_x$-$k_y$ plane. (B and C) Band dispersions along cuts 1 and 2 indicated in (A), recorded with photon energy $h\nu = 22$ and 56 eV, respectively. The solid curves represent the calculated bulk bands along $\Gamma - M$. Note that the chemical potential on the (010) surface is slightly different from that on the (001) surface, most likely because of different surface chemistry effects. (D) Band dispersions along $k_x$ at different $k_y$ positions recorded with different photon energies from 22 to 56 eV. The dashed curve indicates the dispersion of one representative bulk band along $\Gamma - K - M$. (E) Calculated bulk bands along $\Gamma - K - M$. The red curves indicate the calculated bulk bands that correspond to the experimental band dispersion indicated in (D). (F) Near-$E_F$ band dispersions along $k_x$ at different $k_y$ positions recorded with different photon energies from 56 to 78 eV, showing a Dirac-like surface state band along $\Gamma - \bar{x}$. The momentum locations are indicated in (A).
photon energy dependence measurements along $\Gamma - \bar{X}$ on the (010) surface. These measurements map the electronic structure in the $\Gamma - M - K - \Gamma$ plane of the bulk Brillouin zone (BZ). For the bulk states, the measurements on the (010) surface with varying photon energy should be analogous to the in-plane mapping on the (001) surface at a fixed photon energy. In Fig. 3A, the Fermi surface (FS) intensity map obtained by varying photon energy on the (010) surface exhibits enhanced spectral intensity near $\Gamma$, which is consistent with our observation on the (001) surface in Fig. 2A. In addition, the FS intensity map in Fig. 3A shows two straight lines at $k_x = 0$ and $2\pi/(\sqrt{3}a)$ along $\Gamma - M - K - \Gamma$, which is perpendicular to the (010) surface.

To illuminate the origin of the straight-line FSs, we investigate the band dispersions recorded with different photon energies. In Fig. 3B and C, we compare the band dispersions measured along $\Gamma - M$ with the calculated bulk bands. Although most of the experimental band dispersions are in good agreement with the bulk band calculations, we observe an extra feature close to $E_F$ at $k_x = 0$ and $2\pi/(\sqrt{3}a)$, corresponding to the two straight lines in the FS intensity map. Figure 3D illustrates the evolution of the band dispersions upon sliding along the $k_y$ direction. The valence band top at $\Gamma$ gradually sinks upon sliding from $\Gamma$ to $K$, as indicated in Fig. 3D, which is consistent with the calculated bulk bands highlighted by red color in Fig. 3E.
contrast, the extra band is observable near $E_F$ in all the cuts in Fig. 3D, although with weaker spectral intensity around $M$. Figure 3F displays the near-$E_F$ band dispersions obtained with different photon energies. The extra band shows a nearly linear dispersion with the crossing point close to $E_F$. The nondispersive feature of the extra band along $k_p$ (the momentum perpendicular to the surface) indicates its surface origin.

The measurements along $\Gamma - X$ indicate the existence of surface states on the (010) surface, where the hourglass-shaped surface state was predicted to exist. To capture the hourglass fermions and their connectivity to other bands in different directions of the surface BZ, we systematically investigate the low-energy electronic structure of the surface states in the (010) surface BZ in Fig. 4. Let us first review the overall surface band structure in the (010) surface BZ predicted by the calculations. The calculations show two Dirac-like bands that are split in energy along $\Gamma - X$ ($k_x = 0$), leading to two Kramers points with an energy separation of 50 meV at $\Gamma$ (Fig. 4A). These bands are doubly degenerate along $\bar{Z} - \bar{U}$ ($k_x = \pi$) but open a small gap of 10 meV between the upper and lower branches at $\bar{Z}$ (Fig. 4B). The crossing points at $\Gamma$ and $\bar{Z}$ are nothing else but the doubly degenerate end points of the theoretically calculated hourglass-shaped dispersion along $\Gamma - \bar{Z}$ (Fig. 4, C and D).

Along $\Gamma - \bar{X}$, we observe a band splitting from the ARPES intensity plot in Fig. 4E. The band splitting is more discernible in the curvature intensity plot in Fig. 4F. Along $\bar{Z} - \bar{U}$, we observe only one Dirac-like band in Fig. 4 (G and H). These observed band dispersions are generally consistent with the calculated band structures shown in Fig. 4 (A and B). However, some fine features in the calculations remain to be identified. For instance, the band splitting along $\Gamma -\bar{X}$ is only observed below $-0.2$ eV, whereas the paired crossing points at the $\Gamma$ point are not resolved. Moreover, the calculations have predicted a small gap at the $\bar{Z}$ point between the upper and lower branches, which is not resolved experimentally because of an insufficient resolution.

Figure 4I displays the ARPES intensity plot along $\Gamma - \bar{Z}$, where the hourglass fermions theoretically reside. A broad peak disperses from $-150$ meV at $\Gamma$ to $-50$ meV at $\bar{Z}$, which is consistent with the lower branch of the calculated hourglass bands in Fig. 4C. However, the upper branch is difficult to identify in the ARPES intensity data. In Fig. 4J, the curvature intensity plot exhibits a cross-like dispersion, which is consistent with the characteristic of the calculated hourglass fermions in Fig. 4C. However, it should be noted that band dispersions near $E_F$ in the curvature plots suffer interference from the Fermi cutoff, which could lead to some artifacts. We summarize the measured surface band dispersions on the (010) surface in the bottom panel of Fig. 4L. The surface bands along $\Gamma - \bar{Z}$ are connected to the bulk states via Dirac-like bands along $\Gamma - \bar{X}$ and $\bar{Z} - \bar{U}$, indicating the nontrivial topology of surface states. Although the predicted hourglass fermions remain to be completely resolved, the observed (010) surface states are consistent with the global feature of the calculated band structure, thus providing strong evidence for the existence of hourglass fermions.

**CONCLUSION**

By mapping a large set of high-symmetry manifolds in the surface BZ, we provided the first experimental evidence that a newly proposed type of TI, hosting a novel type of surface state, exists in crystals protected by nonsymmorphic symmetry. Most of the symmetry groups in nature are nonsymmorphic and can host interesting topological classes with their own unique surface state responses. Last, nonsymmorphic symmetries can protect bulk semimetals hosting exotic types of fermions (25). All these await experimental discovery.

**MATERIALS AND METHODS**

**Sample growth method**

Single crystals of KHgSb were grown using self-flux methods. The starting materials K (99.95%; Alfa Aesar), Hg (99.9995%; Aladdin), and Sb (antimony shot, 99.999%; Alfa Aesar) were put in an Al$_2$O$_3$ capsule and sealed in a quartz tube. The operation was in a vacuum better than $10^{-11}$ torr.

**ARPES measurement technique**

ARPES measurements were performed at the “Dreamline” beamline of the Shanghai Synchrotron Radiation Facility with a Scienta D80 analyzer. The energy and angular resolutions were set to 15 to 30 meV and 0.2°, respectively. The samples for ARPES measurements were mounted in a BIP argon ($>$99.9999%)–filled glove box, cleaved in situ, and measured at 30 K in a vacuum better than $5 \times 10^{-11}$ torr.

**Calculation method**

The Vienna Ab initio Simulation Package (26) was used for first-principles calculations. The GGA of Perdew-Burke-Ernzerhof type (27) was used for the exchange-correlation potential. Spin-orbit coupling was self-consistently taken into account. The cutoff energy for plane-wave expansion is 500 eV, and the $k$-point sampling grids for different structures were tested to be dense enough. The atomic structure and the lattice constants $a = b = 4.78(4)$ Å and $c = 10.22(5)$ Å were adopted in our calculations (22), which are very close to those determined by our powder XRD data. The KHgSb layers were stacked along the $c$ axis, which is consistent with our experimental observations. The surface Green’s function method was used to calculate the surface states based on the maximally localized Wannier functions (28) of Hg 6s and Sb 5p orbitals obtained from ab initio calculations.

**SUPPLEMENTARY MATERIALS**

Supplementary material for this article is available at http://advances.sciencemag.org/cgi/content/full/3/5/e1602415/DC1

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