

MATERIALS SCIENCE

Predicting short-range order and correlated phenomena in disordered crystalline materials

Eric C. O'Quinn¹, Kurt E. Sickafus², Rodney C. Ewing³, Gianguido Baldinozzi⁴, Joerg C. Neufeind⁵, Matthew G. Tucker⁵, Antonio F. Fuentes⁶, Devon Drey¹, Maik K. Lang^{1*}

Disordered crystalline materials are used in a wide variety of energy-related technologies. Recent results from neutron total scattering experiments have shown that the atomic arrangements of many disordered crystalline materials are not random nor are they represented by the long-range structure observed from diffraction experiments. Despite the importance of disordered materials and the impact of disorder on the expression of physical properties, the underlying fundamental atomic-scale rules of disordering are not currently well understood. Here, we report that heterogeneous disordering (and associated structural distortions) can be understood by the straightforward application of Pauling's rules (1929). This insight, corroborated by first principles calculations, can be used to predict the short-range, atomic-scale changes that result from structural disordering induced by extreme conditions associated with energy-related applications, such as high temperature, high pressure, and intense radiation fields.

INTRODUCTION

Structural disorder in crystalline materials can be engineered for specific functionalities, such as increasing conductivity via chemical doping in semiconductors (1), enhancing flux pinning in high-temperature superconductors (2), and optimizing electrical properties of PZT (lead zirconate titanate perovskite) (3). In these materials, structural properties are commonly studied with techniques that probe the translational periodicity of the atomic constituents over repeating unit cell length scales, such as by x-ray diffraction, and modeled as though atoms may be randomly distributed across their atomic sites. Recently, however, with the development of experimental techniques capable of probing subnanometer length scales, there has been an increased interest in disordered materials for which the actual atomic arrangement is not represented by the periodic structure identified from a diffraction experiment (4). In some disordered oxides, it has been shown that atomic distributions only appear random when sampled over long length scales but are, in fact, ordered at the nanoscale (5, 6). Thus, there is a decoupling of the local symmetry of atomic configurations from the symmetry of the global, long-range structure.

Although discrepancies between short- and long-range structures (7, 8) and a locally ordered distribution of atoms (or vacancies) (9–11) have been reported for disordered crystalline materials, the challenge has been to characterize these materials over multiple length scales. For instance, Shamblin *et al.* (5) investigated a disordered fluorite structure formed by $\text{Ho}_2\text{Zr}_2\text{O}_7$, similar to the structure adopted by yttria-stabilized zirconia ($\text{Y}_x\text{Zr}_{1-x}\text{O}_{2-0.5x}$) and nuclear fuel uranium dioxide (UO_{2+x} + fission products). Using the neutron total scattering method (12), they showed that the local atomic distribution in $\text{Ho}_2\text{Zr}_2\text{O}_7$ is not represented by a disordered fluorite

structure but instead is better explained by a lower-symmetry superstructure of the fluorite structure in which cations and oxygen ions are distributed in a nonrandom manner with concomitant structural distortions. The origin of this short-range ordering is not understood nor is the relation between the short- and long-range atomic configurations. Here, we demonstrate that such heterogeneous structural disorder can be understood by application of Pauling's rules (13, 14). These rules were established on the basis of ordered crystalline structures with atoms placed at ideal positions, in agreement with x-ray diffraction experiments. The same rules, which include a powerful electrostatic principle dictating charge balance, can be applied to predict the intricate short-range atomic ordering schemes and correlated phenomena observed in disordered crystalline materials. This approach advances the current understanding of disordered crystalline materials, as the principle governing balance of ionic charges applies to second nearest neighbor interactions, and Pauling's rules are used in a predictive manner. These predictions are corroborated by neutron total scattering experiments, sensitive to both cation and anion behavior across all spatial scales, and first principles calculations.

RESULTS AND DISCUSSION

To construct an atomic-scale understanding of heterogeneous disorder, we have focused on the complex oxide structures of spinel (rock salt derivative, general formula AB_2O_4 , $Fd-3m$) and pyrochlore (fluorite derivative, general formula $\text{A}_2\text{B}_2\text{O}_7$, $Fd-3m$) as model systems because of their inherent structural disorder (15, 16), a reported discrepancy between the long- and short-range behavior (5, 6), and their importance to many energy-related applications (17, 18). Spinel oxides are isostructural with natural magnesium aluminate (MgAl_2O_4) and are conventionally described by three structural parameters: the isometric unit cell parameter (a), the position of the oxygen anion along the unit cell body diagonal (u), and the inversion parameter (i). Many members of this structural family are disordered, where the two cations are distributed across four-coordinated tetrahedral sites and six-coordinated octahedral sites; the inversion parameter quantifies the fraction of tetrahedral

Copyright © 2020
The Authors, some
rights reserved;
exclusive licensee
American Association
for the Advancement
of Science. No claim to
original U.S. Government
Works. Distributed
under a Creative
Commons Attribution
NonCommercial
License 4.0 (CC BY-NC).

Downloaded from <http://advances.sciencemag.org/> on December 4, 2020

¹Department of Nuclear Engineering, University of Tennessee, Knoxville, TN 37996, USA.

²Department of Materials Science and Engineering, University of Tennessee, Knoxville, TN 37996, USA.

³Department of Geological Sciences, Stanford University, Stanford, CA 94305, USA.

⁴Laboratoire Structures, Propriétés et Modélisation des Solides, CNRS, CentraleSupélec, Université Paris-Saclay, 91190 Gif-sur-Yvette, France.

⁵Neutron Scattering Division, Oak Ridge National Laboratory, Oak Ridge, TN 37831, USA.

⁶Cinvestav-Unidad Saltillo, 25900 Ramos Arizpe, Coahuila, Mexico.

*Corresponding author. Email: mlang2@utk.edu

sites occupied by the B cation. Each oxygen is crystallographically equivalent (Wyckoff equipoint $32e$), bonded to one tetrahedrally coordinated cation and three octahedrally coordinated cations. This structure is indicated by the Bragg peaks in the neutron diffraction pattern (Fig. 1A) with this specific MgAl_2O_4 sample exhibiting an inversion parameter of 38%. According to this structural model, the cation tetrahedra are identical in all ways (i.e., volume, bond lengths, and bond angles), regardless of whether they are occupied by the larger Mg^{2+} (ionic radius^{IV} = 0.57 Å) (19) or smaller Al^{3+} (ionic radius^{IV} = 0.39 Å).

To probe the atomic-scale structure of MgAl_2O_4 , we analyzed the pair distribution function (PDF) collected from a neutron total scattering experiment (Fig. 1B). This experimental approach is well suited for heterogeneously disordered oxides because (i) neutrons scatter strongly from oxygen and generally provide contrast between elements of similar atomic number (e.g., Mg and Al), and (ii) diffuse scattering that arises due to local deviations from the global space group symmetry (12) can be analyzed in real space. The PDF of MgAl_2O_4 is a histogram of atom-atom distances (20). There is an obvious discrepancy between the experimental PDF (Fig. 1B, black circles) and the one simulated from the long-range disordered spinel structural model ($Fd-3m$) obtained from analysis of the neutron diffraction pattern (Fig. 1B, red line) (6). The long-range structural model creates Mg–O and Al–O bond distances ($d_{A-O} = 3a(u - 1/4)$, $d_{B-O} = a [2(u - 3/8)^2 + (5/8 - u)^2]^{1/2}$) (15) that are too short to accurately reproduce the actual interatomic distances observed in the experimental data. This implies that the local atomic arrangement of MgAl_2O_4 is not represented by the disordered, long-range structure. This discrepancy, however, can be reconciled by extending Pauling's rules to disordered spinel. A straightforward application of Pauling's first rule, which states that the cation-anion distance is the sum of the cationic and anionic radii, indicates that the polyhedra in each case should be much different. When the Mg^{2+} occupies the tetrahedral site, the sum of the ionic radii ($\text{O}^{2-,\text{IV}} + \text{Mg}^{2+,\text{IV}}$) is 1.95 Å and when Al^{3+} occupies the tetrahedral site, the sum is 1.77 Å. A hypothetical PDF can be constructed using only Pauling's first rule (Fig. 1B, blue line) that more accurately reproduces the experimental PDF than the long-range disordered spinel model. In this representation, the structural distortion associated with cation inversion is

better accounted for by the incorporation of bond lengths predicted by the first rule.

Cation inversion also leads to complex charge balance schemes. The disordered structure, according to the diffraction pattern analysis, has cations randomly distributed on the cation sublattice, but in reality, each cation polyhedra must be occupied either by Mg^{2+} or by Al^{3+} . When an oxygen is bonded to Mg^{2+} in tetrahedral coordination, then it can also be bonded with zero, one, two, or three other Mg^{2+} in octahedral coordination, and the same four octahedral combinations are available when Al^{3+} is in tetrahedral coordination. Therefore, disordering of the cation sublattice results in eight unique local oxygen environments (Fig. 2). The bond strength (charge divided by coordination number) sum of each of these environments, governed by Pauling's second rule, provides further insight into the local atomic configuration of the disordered phase. When Mg^{2+} occupies the tetrahedral site (~62% occurrence), there is a unique way to locally satisfy this rule: by filling the octahedral sites with Al^{3+} , which is the conventional, "normal" spinel arrangement. When Al^{3+} occupies the tetrahedral site (~38%), there is no way to exactly satisfy the second rule. Pauling gives a prescription for this problem by stating that, while this rule may not be "rigorously satisfied...it should, however, be always satisfied approximately." The most straightforward solution to this problem in a disordered spinel is a simple mixture of the motifs in which the electrostatic valence bond strengths are 2.083 and 1.917, which average to 2. In this scheme, when an oxygen is bonded to an Al^{3+} tetrahedra, it will prefer to be coordinated to two Mg^{2+} and one Al^{3+} octahedra and be nearest neighbors with an oxygen that bonded with an Al^{3+} tetrahedra, one Mg^{2+} , and two Al^{3+} octahedra. This valence consideration explains the atomic arrangement that was revealed by O'Quinn *et al.* (6), in which the local structure around a cation antisite in $\text{Mg}_{1-x}\text{Ni}_x\text{Al}_2\text{O}_4$ was best modeled with a tetragonal unit cell and three unique oxygen positions (Pauling bond strength sums of 2, 2.083, and 1.917). In this case, the lower-symmetry "local phase" contained the necessary short-range atomic ordering and associated relaxations required to satisfy Pauling's rules. Therefore, the PDF of this disordered material is reproduced correctly by accounting for Pauling's first and second rules: The size mismatch of the ions dictates a specific structural distortion away from the long-range

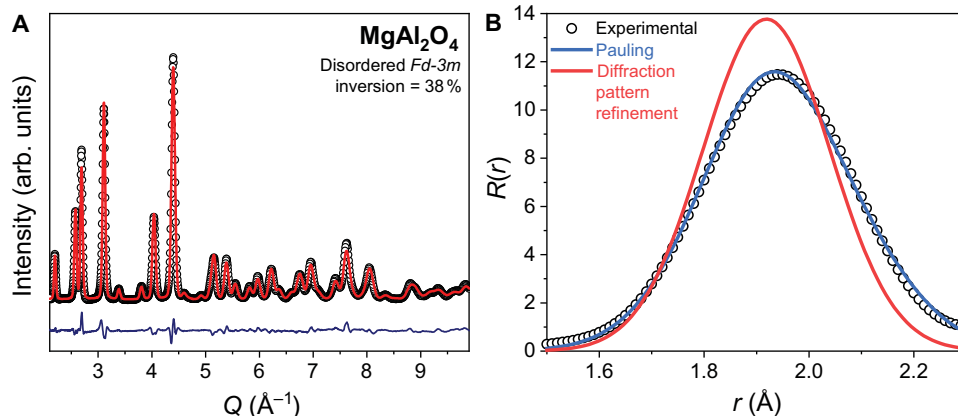


Fig. 1. Neutron total scattering data collected from disordered MgAl_2O_4 . (A) Experimental neutron diffraction pattern (black circles) of MgAl_2O_4 modeled with the disordered spinel structure (red line). (B) Experimental pair distribution function (PDF; black circles) of MgAl_2O_4 compared with a simulated PDF calculated from the model refined from the diffraction pattern (red) and one simulated directly from application of Pauling's first rule (blue) with Shannon's ionic radii.

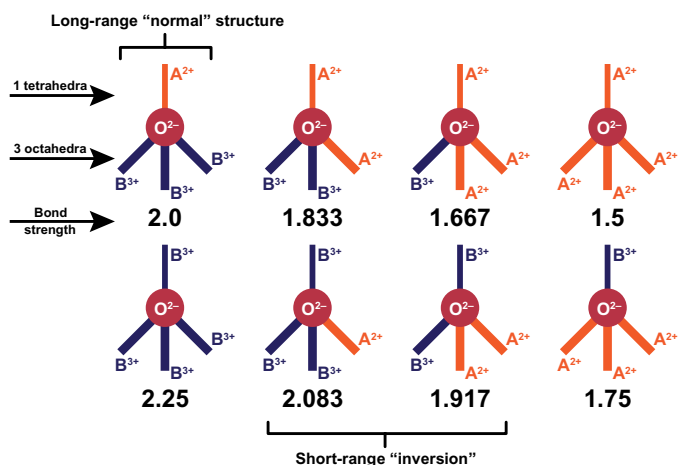


Fig. 2. Schematic representation of the eight possible combinations of oxygen environments in the $A^{2+}B^{3+}_2O^{4-}_2$ spinel structure with their electrostatic valence bond strengths calculated from Pauling's second rule. In this representation, the thinner solid line above the oxygen anion (symbolized as solid red circle) represents the single bond with the tetrahedral site, and the three thicker solid lines below oxygen represent the bonds with the octahedral sites. The orange and dark blue bonds are with A^{2+} and B^{3+} cations, respectively. Only one of the eight possible arrangements produce an electrostatic valence bond strength equal and opposed to that of the oxygen anion satisfying Pauling's valence rule (the normal spinel arrangement, top left).

symmetry (Fig. 1B), and local charge balance dictates a specific distribution of ions within a lower-symmetry structural motif (Fig. 2). The question arises whether Pauling's rules are only useful to understand the local atomic arrangements within a disordered material or whether they can also give fundamental insight into the underlying mechanisms that govern the actual disordering process itself.

To answer this question, we have investigated the pyrochlore-to-fluorite transformation (general formula $A_2B_2O_7$), a classical example of a disordering process. Whereas fluorite oxides (AO_2) contain large, tetravalent cations, there are two cation sites in the pyrochlore structure: an eight-coordinated A site generally occupied by a trivalent rare-earth cation and a six-coordinated B site generally occupied by a tetravalent group 4 element (Fig. 3A) (21); the stability field of the pyrochlore structure has been generally correlated with the cationic radius ratio ($1.46 < r_A^{VIII}/r_B^{VI} < 1.78$). The ordered pyrochlore structure can be driven by irradiation, temperature, pressure, or chemical doping into a disordered state (22, 23), with a disordering process proposed to be driven by cation exchange (24, 25), by randomization of vacancies on the oxygen sublattice (26, 27), or by simultaneous rearrangements on both sublattices (28). Sufficient disordering of the pyrochlore structure ultimately triggers a long-range order-disorder transformation to a fully disordered, anion-deficient fluorite structure ("defect fluorite," $Fm-3m$) (22, 29). The preference of the cations for specific local environments, given by Pauling's rules, helps to identify the atomic-scale disordering sequence, as well as the final atomic arrangement, which is not random but retains some level of predictable order, similar to the behavior observed in spinel. While the disordering of a pyrochlore structure does involve both cation antisite and anion Frenkel defects (22), it can be surmised by application of Pauling's first rule that cation sublattice disorder is driven by an anion sublattice disordering

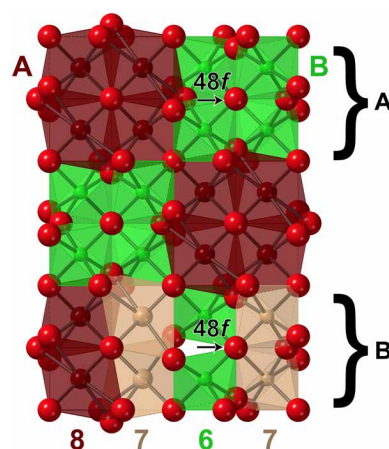


Fig. 3. Schematic illustration of cation coordination. (A) before and (B) after the motion of an oxygen anion from the 48f to the 8a Wyckoff equipoint in the pyrochlore structure. The dark brown polyhedra are eight-coordinated, the light brown polyhedra are seven-coordinated, and the green polyhedra are six-coordinated. The viewing direction is $[100]_{Fd-3m}$.

mechanism (fluorite-related structures are generally oxygen ion conductors) (18). Without a precursor oxygen defect, the sizes of the cation coordination polyhedra are simply too large (or small) to accommodate a stable cation antisite defect. In contrast, the motion of the 48f oxygen to the previously vacant 8a site creates a distinct pattern of cation coordination geometries in the local environment around the Frenkel defect (an "8-7-6-7" arrangement; Fig. 3B). Whereas, previously, the tri- and tetravalent cations had a preference for occupying the large, eight-coordinate and small, six-coordinate sites, respectively, newly created seven-coordinate sites (more appropriate in size for both A^{3+} and B^{4+}) become available for the formation of cation antisite defects via the motion of the oxygen anion. This scenario is in excellent agreement with previous *ab initio* studies on pyrochlore oxides that showed that oxygen migration facilitates the disordering process (30, 31). However, in contrast to the traditional long-range picture of a complete cation randomization into only seven-coordinated polyhedra, part of the initial coordination polyhedra are retained in the local structure of the disordered phase. In the traditional structural approach, it is not easy to unambiguously determine how many of the original polyhedra are retained in the new structural motif or how far this motif extends into the ordered matrix. This can be better conceptualized in the framework of the structural building blocks that form the ordered structure and their change through the motion of oxygen into the vacant site. The pyrochlore structure can be built using a layer stacking model (32) that consists of an A_3B layer, a Kagome lattice of A^{VIII} cations with B^{VI} cations occupying the interstices (Fig. 4A), and an AB_3 layer, a Kagome lattice of B^{VI} cations with A^{VIII} cations occupying the interstices (Fig. 4B). The building blocks that produce these layers (33) are arrangements of A_3B (8-8-8-6 motif) and AB_3 (6-6-6-8 motif) polyhedra (Fig. 4C). These blocks can be understood in terms of Pauling's rules as fundamental units with particularly stable polyhedral configurations. The disordering process induced by movement of the 48f oxygen into the vacant 8a site now changes the polyhedra and cation coordination scheme of the building blocks to an 8-7-7-6 motif in the A_3B layer and a 6-7-7-8 motif in the AB_3 layer (Fig. 4D). Thus, the six-coordinated sites are now highly distorted, ideally

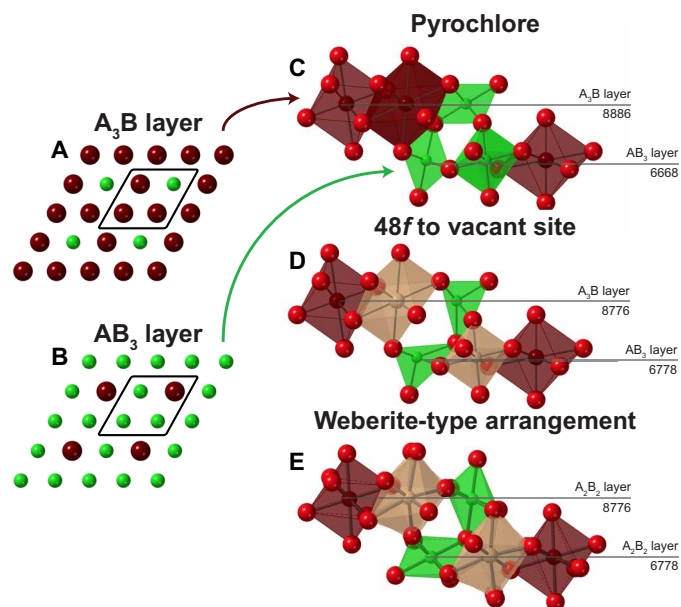


Fig. 4. Two cation layers comprise the layer stacking model (32) that describes the pyrochlore structure. The fundamental building blocks contained within these two layers comprising the layer stacking model, (A) an A_3B layer and an (B) AB_3 layer, are shown (C) before and (D) after the motion of an oxygen anion from the 48f to the 8a Wyckoff equi-point. The cation coordination scheme is compared with (E) the DFT-relaxed weberite-type arrangement of $Ho_2Zr_2O_7$. The dark brown polyhedra are eight coordinated, the light brown polyhedra are seven coordinated, and the green polyhedra are six coordinated. The viewing directions for (A) and (B) are $[1\ 1\ 1]_{Fd-3m}$, $[0\ -1\ 1]_{Fd-3m}$ for (C) and (D), and $[0\ 1\ 0]_{C21/m}$ for (E).

prompting a subsequent relaxation of other oxygen. Interestingly, the 8-7-7-6 motif of coordination polyhedra is characteristic for weberite-type Y_3TaO_7 ($C222_1$). This explains why a weberite-type structure has been previously shown to accurately model the local structure of a material that adopts the disordered, anion-deficient fluorite structure (5). The $C222_1$ space group, in particular, best describes the experimental neutron PDF of the disordered, anion-deficient fluorite $Ho_2Zr_2O_7$ (fig. S1) with the difference that the seven-coordinated polyhedra are populated by both Ho^{3+} and Zr^{4+} cations (only Y^{3+} for Y_3TaO_7). This Pauling-inspired building block approach also has practical applications. Using the fundamental building blocks of the pyrochlore and weberite-type structure, we constructed primitive cells for first principles calculations, which reveal that a local structure containing weberite-type building blocks (Fig. 4E) is a lower-energy configuration for $Ho_2Zr_2O_7$ than a local structure containing pyrochlore building blocks with only eight and six coordination; the reverse is true for $Ho_2Ti_2O_7$ (table S1). Even after removing the constraints of the weberite-type symmetry on $Ho_2Zr_2O_7$, the relaxation of this atomic arrangement converges to the same energy (-198.811 eV) with a nearly identical configuration. The density functional theory (DFT) calculations also show how the previously distorted six-coordinated octahedra that are distorted by the oxygen motion are now relaxed such that the two polar oxygen form a $\sim 180^\circ$ angle (as was the case with ordered pyrochlore). With the application of Pauling's rules to the disordering process of pyrochlore, the local weberite-type polyhedral motif can be fully explained.

What remains to be understood for a full description of the heterogeneous disorder in pyrochlore oxides is the relation between

the weberite-type local structural motifs and the long-range disordered, anion-deficient fluorite structure. While the weberite-type structural motifs are induced over a subnanometer length scale, they still scatter neutrons (or x-rays) coherently. A crystallographic approach developed by Neder *et al.* (34) considers these structural motifs as ordered variants inserted in a host crystal that is the configuration average of all possible orientations (phases) of the domains. One can show with a detailed crystallographic analysis that the sharp Bragg intensities correspond to the reciprocal lattice points of the host crystal, while diffuse scattering is induced by the correlated differences between each domain structure and the average host crystal structure. This approach explains, based on group theory, that an ensemble of subnanoscale weberite structural motifs ($C222_1$) with all possible orientations (formed by random movement of different 48f oxygens into vacant 8a sites) will become, on average, an anion-deficient fluorite structure ($Fm-3m$) over longer length scales, resulting in the extinction of all superstructure peaks (Supplementary Materials). Thus, the disordering process in pyrochlore can be understood as an accumulation of local weberite-type structural motifs that form a long-range anion-deficient fluorite structure, yielding the observed heterogeneous structure over different length scales. Through a solid-solution series that covers the entire order-disorder space from fully ordered pyrochlore ($Ho_2Ti_2O_7$) to fully disordered, anion-deficient fluorite ($Ho_2Zr_2O_7$), we have investigated whether the order-to-disorder transformation proceeds over different length scales simultaneously. Neutron total scattering experiments were performed on intermediate members of the solid solution binary $Ho_2(Ti_{1-x}Zr_x)_2O_7$. The neutron diffraction data reveal that there is a narrow compositional range over which the series transforms from the pyrochlore structure to the disordered, anion-deficient fluorite structure (Fig. 5, black line). By contrast, the local weberite-type phase forms immediately upon substitution of Zr for Ti, and the fraction increases nearly linearly with the amount of Zr across the series (Fig. 5, red line). Thus, there is an apparent decoupling of the local weberite-type formation in $Ho_2(Ti_{1-x}Zr_x)_2O_7$ that proceeds gradually upon substitution for Ti^{4+} with Zr^{4+} , while the long-range anion-deficient fluorite phase forms only within a narrow compositional range of about $\sim 60\%$ substitution. Again, Pauling's rules are key to explain this complex and intriguing disordering scheme. Once an oxygen is moved into a vacant site and a sevenfold Zr^{4+} site is created, this limits the movement of other nearby oxygens; another oxygen must not move to be also coordinated with this newly created sevenfold Zr^{4+} site. Thus, the newly formed local environment dictates how the construction of the material must proceed over longer length scales. To obey Pauling's rules, the local weberite domains will maintain a critical distance until a certain critical density is reached, which triggers a long-range phase transformation. A similar behavior has been observed in phase transformations induced by heavy ion irradiation of A_2O_3 oxides (35) in which oxygen vacancies are created and arrange themselves as far away from one another as possible until saturation triggers a global phase transformation. The present data can be interpreted in the same way, particularly as the fundamental weberite-type structural motif is just, in principle, the short-range ordering and structural relaxations associated with an anion Frenkel defect (Fig. 4E).

As structural disorder is highly correlated with the expression of physical properties, this new insight has implications for engineering materials over different length scales to obtain the desired physical

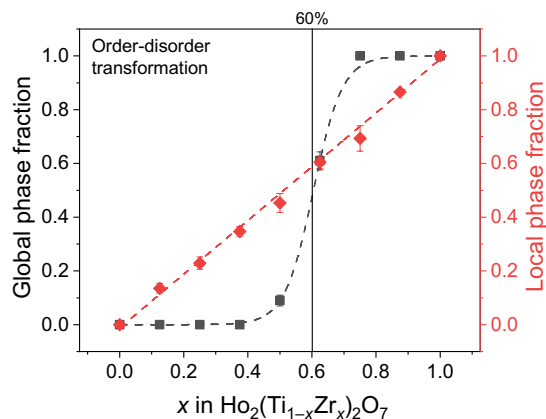


Fig. 5. The locally ordered weberite-type (red diamonds) versus global, disordered, anion-deficient fluorite phase fractions (black squares), obtained from small-box and Rietveld refinements of neutron total scattering data, respectively, from $\text{Ho}_2\text{Ti}_{2-x}\text{Zr}_x\text{O}_7$ pyrochlore. Dashed lines are included to guide the eye.

properties for technologically important applications. The promise of manipulating the specific local environment of a material that appears randomly disordered can be appreciated with the example of PZT perovskite. The origin of enhanced piezoelectricity in PZT has remained largely a mystery since the 1950s due to the complex phase diagram of the material (36). Recent work has suggested that piezoelectricity in PZT may be explained by the growth of nanoscale low-symmetry domains that average to a different higher-symmetry structure over longer length scales (37). Within a certain compositional range, the substitution of Zr^{4+} for Ti^{4+} modifies local cation environments and increases the piezoelectric response without altering the observed long-range symmetry (7). The fact that the local structure of such a disordered material can now be interpreted as a result of fundamental known chemical rules is relevant for next-generation materials engineering. In pyrochlore oxides, the propensity of the structure to disorder has been linked with increased oxygen conductivity (38), improved performance in radiation fields (39), and the emergence of exotic magnetic properties such as spin ice behavior (40). This study has provided the basis not only to understand these phenomena in terms of the underlying atomic arrangement but also how to manipulate the structure across different length scales to induce desired material properties.

Pauling's original formulations were based on the nature of chemical bonds between ions (41), a very short-range interaction dictated by quantum mechanics (42). Thus, it is therefore not unexpected that a disordering mechanism will not violate these fundamental chemical rules. Once disorder is induced via some internal (e.g., doping) or external (e.g., irradiation, pressure, and mechanical action) mechanism, the atomic structure will rearrange itself to a specific configuration that is a direct consequence of Pauling's rules. For example, inversion in spinel or cation antisite defects in pyrochlore is not just simply switching atoms, which would violate these rules, but instead new sites are created that accommodate the size and charge of the cations. Thus, this rearrangement and its consequences for both the short- and long-range structures can be correctly predicted by Pauling's rules: Rule 1 determines how far apart atoms are and how many neighbors atoms have, rule 2 determines how unlike ions balance charge with one another, rules 3 and 4 determine how like ions repel charges from one another, and rule 5

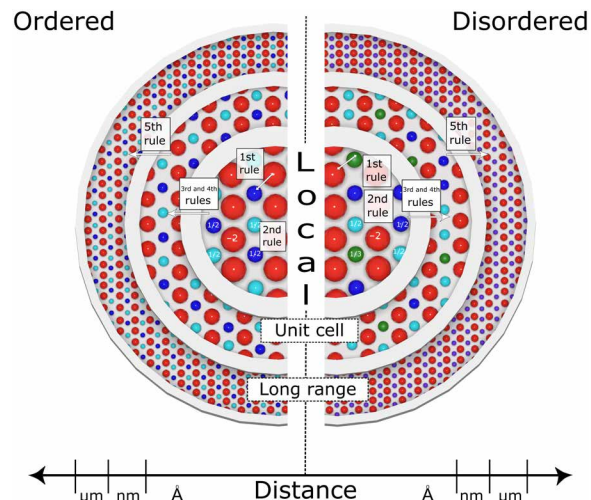


Fig. 6. Schematic illustration of atomic arrangements in ordered (left) and disordered (right) ionic materials. The red circles represent anions, and the different blue and green circles represent unique cation species. When a material that appears structurally disordered over longer length scales is studied at the atomic-scale, the actual atomic configuration and accompanying structural distortions obey Pauling's rules. The rules are labeled for the length scales over which they are primarily applicable.

is a restatement of Occam's razor—the complexity of the structure should be a minimum. The examples discussed in this study were predominately explained with Pauling's first and second rules, which describe highly local phenomena: the distances between ions, the coordination polyhedra they form, and the way that unlike ions balance charges. Rules 3 to 5 were used to verify the obtained structural models. While we have shown the examples of the behavior of spinel and pyrochlore structures, we have experimental data that show the same behavior for doped ThO_2 , A_2BO_5 oxides, and A_3BO_7 oxides. Furthermore, this complexity has been observed in materials disordered by nonstoichiometry (43), intense radiation (10), mechanochemical synthesis (44), or temperature exposure (45). This demonstrates that the new disordering concept presented in this study is, as Pauling's rules were for ordered ionic compounds, a general phenomenon for a wide range of disordered materials independent on how the disorder is introduced. This knowledge is important, as the specific short-range atomic configurations in these materials are no longer represented by the observable long-range structure. If disorder occurs in a crystalline material, then Pauling's rules can be used to predict which atoms move from their ideal positions to their final arrangement within the disordered phase (Fig. 6). This atomic-scale process is not random, as would be suggested by the structural behavior over longer length scales, but involves a high level of order that must be considered when designing materials for energy-related applications.

MATERIALS AND METHODS

Neutron total scattering

Oxide materials for this study were prepared via conventional solid-state methods. Structural characterization was performed at the Nanoscale-Ordered Materials Diffractometer (NOMAD) beamline (46) of Oak Ridge National Laboratory's Spallation Neutron Source.

Polycrystalline powders (100 to 150 mg) of each sample were placed in quartz capillaries and exposed to the thermal neutron beam. Scattering background was accounted for by subtracting the scattering data collected from an empty quartz capillary of identical dimension measured for an identical length of time to the sample of interest. The total scattering structure function, $S(Q)$, was produced by normalizing the background-corrected scattering data to neutron scattering from vanadium (to account for the neutron spectrum). Using STOG (47), the PDF, $G(r)$, was obtained from the structure function, $S(Q)$, via Fourier transform

$$G(r) = 4\pi r \rho_0 [g(r) - 1] = \frac{2}{\pi} \int Q [S(Q) - 1] \sin(Qr) dQ \quad (1)$$

where the integral was carried out over a Q range of 0.2 to 31.4 \AA^{-1} . The magnitude of the scattering vector, Q , is given by

$$Q = \frac{4\pi \sin \theta}{\lambda} \quad (2)$$

where λ is the neutron wavelength. The PDF, $g(r)$, is related to the radial distribution function (RDF), $R(r)$ (20), by

$$R(r) = 4\pi r^2 \rho_0 g(r) \quad (3)$$

where ρ_0 is the sample atomic density.

X-ray total scattering

X-ray total scattering was performed at the 28-ID-2 X-ray Powder Diffraction (XPD) beamline at the National Synchrotron Light Source-II (48) at Brookhaven National Laboratory. $\text{Ho}_2\text{Zr}_2\text{O}_7$ powder was investigated at room temperature in a Kapton tube capillary with an exposure time of 10 s and photon wavelength of 0.18754 \AA (~66.1 keV). An empty Kapton tube and a LaB_6 standard were measured to correctly subtract the capillary's scattering as background, scale the sample's scattering intensity correctly, and determine the instrument parameters for use in structural refinement software. The scattering from the sample was recorded as a two-dimensional (2D) diffractogram gathered using a PerkinElmer XRD 1621 digital imaging detector. The structure function $S(Q)$ was extracted from the resulting 2D diffraction image, with the scattering vector Q varying from $Q_{\min} = 0.5 \text{\AA}^{-1}$ to $Q_{\max} = 25.0 \text{\AA}^{-1}$. The PDF, $G(r)$, was obtained using the software PDFgetX3 (49) via the relation

$$G(r) = r \left(A \int_{Q_{\min}}^{Q_{\max}} Q [S(Q) - 1] \sin(Qr) dQ \right) \quad (4)$$

Total scattering data were analyzed by a variety of methods including Rietveld and small-box refinement. General Structure Analysis System (GSAS) I (50) and GSAS II (51) were used to perform Rietveld refinement of the diffraction patterns, in which refined parameters included vertical scale, unit cell parameters, atomic positions, atomic displacement parameters, and site occupancies when appropriate. PDFgui (52) was used to perform small-box refinements of the PDFs; in addition to the same parameters that are refined during Rietveld refinements, another parameter was refined to account for correlated atomic motion that has the effect of sharpening the peaks in low r . Additional details concerning the small-box refinement of disordered spinel and fluorite oxides can be found elsewhere (5, 6). Simulated RDFs were calculated using the relation

$$\text{Coordination number} = \int R(r) dr \quad (5)$$

accounting for the fact that the total RDF is composed of contributions from partial pair correlations, which are weighted by the product of the neutron scattering lengths and concentrations of the atoms that comprise the pair.

First principles calculations

To identify the thermodynamically stable forms of $\text{Ho}_2\text{Zr}_2\text{O}_7$ and $\text{Ho}_2\text{Ti}_2\text{O}_7$ and the different atomic arrangements, we calculated the relative stabilities of four different phases by first principles calculations: pyrochlore, weberite (*Imma*), and two weberite-type arrangements derived by the $C222_1$ structure of Y_3TaO_7 . The electronic structure calculations are performed within the DFT framework using the projector augmented wave approach (53) for the core-valence interaction and the general gradient approximation with Perdew-Burke-Ernzerhof (PBE)-generalized gradient approximation (CGA) (54) for the exchange-correlation functional as implemented in the Vienna Ab initio Simulation Package (VASP) code (55).

The potentials use 9 valence electrons for Ho, 12 for Ti, 12 for Zr, and 6 for O. A plane wave kinetic energy cutoff was determined at 520 eV, with a uniform k -point mesh for Brillouin zone sampling, adapted to each specific symmetry, based on the Monkhorst-Pack scheme (56) that was found to be sufficient to achieve well-converged energies. Electronic self-consistency was considered achieved when the total energy change between electronic steps is less than $\leq 1 \mu\text{eV}$. The lattice metric was relaxed for all crystal symmetries, and the internal structural parameters were relaxed until all Hellmann-Feynman forces on each ion were $\leq 2 \text{ meV/\AA}$.

After the initial structural optimizations using the PBE GGA functionals, calculations were performed using GGA + U functionals within the simplified rotationally invariant approach introduced by Dudarev *et al.* (57) to take into account the strongly correlated nature of the f -states of Holmium. In those calculations, we used a Ho potential with 21 valence electrons. A (U-J) value of 5.4 eV was found to be a good compromise for all structures. The value was obtained using the linear response ansatz (58) and is in good agreement with previous reports in the literature for lanthanide systems (43, 59, 60).

The primitive structure of the weberite-type structure can be used as a starting point for modeling the $\text{A}_2\text{B}_2\text{O}_7$ compounds. Obviously, the change of stoichiometry from A_3BO_7 to $\text{A}_2\text{B}_2\text{O}_7$ destroys part of the symmetries of the structure. In the weberite-type A_3BO_7 structures, a quarter of the cations occupy the B site and are bonded to six O atoms, forming an octahedron. Another quarter of the cations occupy an A-type site and are bonded to eight O atoms, a polyhedron that can be described as a distorted cube. The remaining half of the A-type cations occupy the remaining A-type sites that are bonded to seven O atoms. A reasonable choice is to use half of the sevenfold-bonded A-type site to accommodate the surplus of B cations of the $\text{A}_2\text{B}_2\text{O}_7$ compound. There are two simple non-equivalent choices for distributing the B cations onto the sevenfold coordinated sites in an ordered way.

The first type of weberite-type structure corresponds to filling M1 and M2 sites with B-type ions. The other type of structure is created by filling M1 and M3 sites with B-type ions. The resulting symmetries in the conventional orthorhombic lattices are quite different. The DFT calculations were performed in primitive structures containing two chemical formulas of the compound. A uniform k -point mesh ($6 \times 6 \times 5$) for Brillouin zone sampling based on the Monkhorst-Pack scheme (56), corresponding to 54 irreducible

points for the type 1 structure and to 36 points for the type 2 structure, was found to be sufficient to achieve well-converged energies. The space group of the type 1 structure is monoclinic $C21/m$. Unfortunately, this group does not exist in the International Tables of Crystallography (ITC), so we can only use the simple monoclinic subgroup $P21/m$ to describe the type 1 structure in a standard way. The direct consequence of this choice is that the list of independent atoms doubles, because each atom in the structure is duplicated by the explicit expression of the C-centering. The space group of the type 2 structure, obtained transforming the primitive lattice back to the conventional representation of weberite-type structures, is orthorhombic $C2mm$ (group number 38 in ITC) but with an origin shift (0 0 1).

SUPPLEMENTARY MATERIALS

Supplementary material for this article is available at <http://advances.sciencemag.org/cgi/content/full/6/35/eabc2758/DC1>

REFERENCES AND NOTES

- E. F. Schubert, Doping in III-V Semiconductors. *Phys. Today* **47**, 71 (1994).
- L. Civalè, A. D. Marwick, T. K. Worthington, M. A. Kirk, J. R. Thompson, L. Krusin-Elbaum, Y. Sun, J. R. Clem, F. Holtzberg, Vortex confinement by columnar defects in $\text{YBa}_2\text{Cu}_3\text{O}_7$ crystals: Enhanced pinning at high fields and temperatures. *Phys. Rev. Lett.* **67**, 648–651 (1991).
- N. Izyumskaya, Y.-I. Alivov, S.-J. Cho, H. Morkoç, H. Lee, Y.-S. Kang, Processing, structure, properties, and applications of PZT thin films. *Crit. Rev. Solid State Mater. Sci.* **32**, 111–202 (2007).
- D. A. Keen, A. L. Goodwin, The crystallography of correlated disorder. *Nature* **521**, 303–309 (2015).
- J. Shamblyn, M. Feyngenson, J. Neuefeind, C. L. Tracy, F. Zhang, S. Finkeldei, D. Bosbach, H. Zhou, R. C. Ewing, M. Lang, Probing disorder in isometric pyrochlore and related complex oxides. *Nat. Mater.* **15**, 507–511 (2016).
- E. C. O'Quinn, J. Shamblyn, B. Perlov, R. C. Ewing, J. Neuefeind, M. Feyngenson, I. Gussev, M. Lang, Inversion in $\text{Mg}_{1-x}\text{Ni}_x\text{Al}_2\text{O}_4$ Spinel: New insight into local structure. *J. Am. Chem. Soc.* **139**, 10395–10402 (2017).
- N. Zhang, H. Yokota, A. M. Glazer, Z. Ren, D. A. Keen, D. S. Keeble, P. A. Thomas, Z.-G. Ye, The missing boundary in the phase diagram of $\text{PbZr}_{1-x}\text{Ti}_x\text{O}_3$. *Nat. Commun.* **5**, 5231 (2014).
- S. Hull, S. T. Norberg, M. G. Tucker, S. G. Eriksson, C. E. Mohn, S. Stølen, Neutron total scattering study of the δ and β phases of Bi_2O_3 . *Dalt. Trans.*, 8737–8745 (2009).
- G. King, C. M. Thompson, J. E. Greedan, A. Lobet, Local structure of the vacancy disordered fluorite Yb_3TaO_7 from neutron total scattering. *J. Mater. Chem. A*, **1**, 10487–10494 (2013).
- J. Shamblyn, C. L. Tracy, R. I. Palomares, E. C. O'Quinn, R. C. Ewing, J. Neuefeind, M. Feyngenson, J. Behrens, C. Trautmann, M. Lang, Similar local order in disordered fluorite and aperiodic pyrochlore structures. *Acta Mater.* **144**, 60–67 (2018).
- S. T. Norberg *et al.*, Pyrochlore to fluorite transition: The $\text{Y}_2(\text{Ti}_{1-x}\text{Zr}_x)_2\text{O}_7$ ($0.0 \leq x \leq 1.0$) system. *Chem. Mater.* **24**, 4294–4300 (2012).
- M. T. Dove, M. G. Tucker, D. A. Keen, Neutron total scattering method: Simultaneous determination of long-range and short-range order in disordered materials. *Eur. J. Mineral.* **14**, 331–348 (2002).
- L. Pauling, The principles determining the structure of complex ionic crystals. *J. Am. Chem. Soc.* **51**, 1010–1026 (1929).
- L. Pauling, *The Nature of the Chemical Bond* (Cornell Univ. Press, Ithaca, NY, ed. 3, 1960), pp. 505–562.
- K. E. Sickafus, J. M. Wills, N. W. Grimes, Structure of spinel. *J. Am. Ceram. Soc.* **82**, 3279–3292 (1999).
- L. Minervini, R. W. Grimes, K. E. Sickafus, Disorder in pyrochlore oxides. *J. Am. Ceram. Soc.* **83**, 1873–1878 (2000).
- C. Yuan, H. Bin Wu, Y. Xie, X. W. Lou, Mixed transition-metal oxides: Design, synthesis, and energy-related applications. *Angew. Chemie - Int. Ed.* **53**, 1488–1504 (2014).
- A. Navrotsky, Thermodynamics of solid electrolytes and related oxide ceramics based on the fluorite structure. *J. Mater. Chem.* **20**, 10577–10587 (2010).
- R. D. Shannon, Revised effective ionic radii and systematic studies of interatomic distances in halides and chalcogenides. *Acta Cryst.* **32**, 751–767 (1976).
- T. Egami, S. J. Billinge, *Underneath the Bragg Peaks* (Pergamon Press, 2003), vol. 6.
- M. A. Subramanian, G. Aravamudan, G. V. Subba Rao, Oxide pyrochlores - A review. *Prog. Solid State Chem.* **15**, 55–143 (1983).
- R. C. Ewing, W. J. Weber, J. Lian, Nuclear waste disposal-pyrochlore ($\text{A}_2\text{B}_2\text{O}_7$): Nuclear waste form for the immobilization of plutonium and "minor" actinides. *J. Appl. Phys.* **95**, 5949–5971 (2004).
- F. X. Zhang, J. W. Wang, J. Lian, M. K. Lang, U. Becker, R. C. Ewing, Phase stability and pressure dependence of defect formation in $\text{Gd}_2\text{Ti}_2\text{O}_7$ and $\text{Gd}_2\text{Zr}_2\text{O}_7$ pyrochlores. *Phys. Rev. Lett.* **100**, 045503 (2008).
- P. J. Wilde, C. R. A. Catlow, Defects and diffusion in pyrochlore structured oxides. *Solid State Ion.* **112**, 173–183 (1998).
- W. R. Panero, L. Stixrude, R. C. Ewing, First-principles calculation of defect-formation energies in the $\text{Y}_2(\text{Ti},\text{Sn},\text{Zr})_2\text{O}_7$ pyrochlore. *Phys. Rev. B* **70**, 054110 (2004).
- C. Heremans, B. J. Wuensch, J. K. Stalick, E. Prince, Fast-ion conducting $\text{Y}_2(\text{Zr}_y\text{Ti}_{1-y})_2\text{O}_7$ pyrochlores: Neutron rietveld analysis of disorder induced by Zr substitution. *J. Solid State Chem.* **117**, 108–121 (1995).
- M. P. van Dijk, A. J. Burggraaf, A. N. Cormack, C. R. A. Catlow, Defect structures and migration mechanisms in oxide pyrochlores. *Solid State Ion.* **17**, 159–167 (1985).
- P. Nachimuthu, S. Thevuthasan, E. M. Adams, W. J. Weber, B. D. Begg, B. S. Mun, D. K. Shuh, D. W. Lindle, E. M. Gullikson, R. C. C. Perera, Near-edge X-ray absorption fine structure study of disordering in $\text{Gd}_2(\text{Ti}_{1-x}\text{Zr}_x)_2\text{O}_7$ pyrochlores. *J. Phys. Chem. B* **109**, 1337–1339 (2005).
- K. E. Sickafus, L. Minervini, R. W. Grimes, J. A. Valdez, M. Ishimaru, F. Li, K. J. McClellan, T. Hartmann, Radiation tolerance of complex oxides. *Science* **289**, 748–751 (2000).
- Y. Li, P. M. Kowalski, Energetics of defects formation and oxygen migration in pyrochlore compounds from first principles calculations. *J. Nucl. Mater.* **505**, 255–261 (2018).
- Y. Li, P. M. Kowalski, G. Beridze, A. R. Birnie, S. Finkeldei, D. Bosbach, Defect formation energies in $\text{A}_2\text{B}_2\text{O}_7$ pyrochlores. *Scr. Mater.* **107**, 18–21 (2015).
- K. E. Sickafus, R. W. Grimes, S. M. Corish, A. R. Cleave, M. Tang, C. R. Stanek, B. P. Uberuaga, J. A. Valdez, Layered Atom Arrangements in Complex Materials. Los Alamos Series Report # LA-14205 (2005).
- L. Cai, J. C. Nino, Complex ceramic structures. I. Weberites. *Acta Cryst. Sect. B* **65**, 269–290 (2009).
- R. B. Neder, F. Frey, H. Schulz, Diffraction theory for diffuse scattering by correlated microdomains in materials with several atoms per unit cell. *Acta Cryst. Sect. A* **46**, 792–798 (1990).
- C. L. Tracy, M. Lang, F. Zhang, C. Trautmann, R. C. Ewing, Phase transformations in Ln_2O_3 materials irradiated with swift heavy ions. *Phys. Rev. B* **92**, 174101 (2015).
- H. Jaffe, Piezoelectric Ceramics. *J. Am. Ceram. Soc.* **41**, 494–498 (1958).
- A. M. Glazer, P. A. Thomas, K. Z. Baba-Kishi, G. K. H. Pang, C. W. Tai, Influence of short-range and long-range order on the evolution of the morphotropic phase boundary in $\text{Pb}(\text{Zr}_{1-x}\text{Ti}_x)\text{O}_3$. *Phys. Rev. B* **70**, 184123 (2004).
- F. Yang, Y. Wang, X. Zhao, P. Xiao, Enhanced ionic conductivity in pyrochlore and fluorite mixed phase yttrium-doped lanthanum zirconate. *J. Power Sources* **273**, 290–297 (2015).
- B. P. Uberuaga, M. Tang, C. Jiang, J. A. Valdez, R. Smith, Y. Wang, K. E. Sickafus, Opposite correlations between cation disordering and amorphization resistance in spinels versus pyrochlores. *Nat. Commun.* **6**, 8750 (2015).
- S. T. Bramwell, M. J. P. Gingras, Spin ice state in frustrated magnetic pyrochlore materials. *Science* **294**, 1495–1501 (2001).
- J. George, D. Waroquiers, D. D. Stefano, G. Petretto, G.-M. Rignanese, G. Hautier, The limited predictive power of the Pauling rules. *Angew. Chemie Int. Ed. Engl.* **59**, 7569–7575 (2020).
- L. Pauling, The sizes of ions and the structure of ionic crystals. *J. Am. Chem. Soc.* **49**, 765–790 (1927).
- S. Finkeldei, P. Kegler, P. M. Kowalski, C. Schreinemachers, F. Brandt, A. A. Bukaemskiy, V. L. Vinograd, G. Beridze, A. Shelyug, A. Navrotsky, D. Bosbach, Composition dependent order-disorder transition in $\text{Nd}_x\text{Zr}_{1-x}\text{O}_{2-0.5x}$ pyrochlores: A combined structural, calorimetric and *ab initio* modeling study. *Acta Mater.* **125**, 166–176 (2017).
- E. C. O'Quinn, J. L. Bishop, R. Sherrod, J. Neuefeind, S. M. Montemayor, A. F. Fuentes, M. Lang, Advanced characterization technique for mechanochemically synthesized materials: Neutron total scattering analysis. *J. Mater. Sci.* **53**, 13400–13410 (2018).
- C.-K. Chung, J. Shamblyn, E. C. O'Quinn, A. Shelyug, I. Gussev, M. Lang, A. Navrotsky, Thermodynamic and structural evolution of $\text{Dy}_2\text{Ti}_2\text{O}_7$ pyrochlore after swift heavy ion irradiation. *Acta Mater.* **145**, 227–234 (2018).
- J. Neuefeind, M. Feyngenson, J. Carruth, R. Hoffmann, K. K. Chipley, The nanoscale ordered MAterials diffractometer NOMAD at the spallation neutron source SNS. *Nucl. Instrum. Methods Phys. Res. B* **287**, 68–75 (2012).
- M. G. Tucker, D. A. Keen, M. T. Dove, A. L. Goodwin, Q. Hui, RMCProfile: Reverse Monte Carlo for polycrystalline materials. *J. Phys. Condens. Matter* **19**, 335218 (2007).
- X. Shi, S. Ghose, E. Dooryhee, Performance calculations of the X-ray powder diffraction beamline at NSLS-II. *J. Synchrotron Radiat.* **20**, 234–242 (2013).
- P. Juhás, T. Davis, C. L. Farrow, S. J. L. Billinge, PDFgetX3: A rapid and highly automatable program for processing powder diffraction data into total scattering pair distribution functions. *J. Appl. Cryst.* **46**, 560–566 (2013).

50. A. C. Larson, R. B. Von Dreele, General Structure Analysis System (GSAS). *Los Alamos Lab. Rep.* **748**, 86–748 (1994).
51. B. H. Toby, R. B. Von Dreele, GSAS-II: The genesis of a modern open-source all purpose crystallography software package. *J. Appl. Cryst.* **46**, 544–549 (2013).
52. C. L. Farrow, P. Juhas, J. W. Liu, D. Bryndin, E. S. Božin, J. Bloch, T. Proffen, S. J. L. Billinge, PDFfit2 and PDFgui: Computer programs for studying nanostructure in crystals. *J. Phys. Condens. Matter* **19**, 335219 (2007).
53. G. Kresse, D. Joubert, From ultrasoft pseudopotentials to the projector augmented-wave method. *Phys. Rev. B.* **59**, 1758–1775 (1999).
54. J. P. Perdew, K. Burke, M. Ernzerhof, Generalized gradient approximation made simple. *Phys. Rev. Lett.* **77**, 3865–3868 (1996).
55. G. Kresse, J. Furthmüller, Efficient iterative schemes for *ab initio* total-energy calculations using a plane-wave basis set. *Phys. Rev. B.* **54**, 11169–11186 (1996).
56. H. J. Monkhorst, J. D. Pack, Special points for Brillouin-zone integrations. *Phys. Rev. B.* **13**, 5188–5192 (1976).
57. S. L. Dudarev, G. A. Botton, S. Y. Savrasov, C. J. Humphreys, A. P. Sutton, Electron-energy-loss spectra and the structural stability of nickel oxide: An LSDA+U study. *Phys. Rev. B - Condens. Matter Mater. Phys.* **57**, 1505–1509 (1998).
58. M. Cococcioni, S. De Gironcoli, Linear response approach to the calculation of the effective interaction parameters in the LDA+U method. *Phys. Rev. B* **71**, 35105 (2005).
59. A. Blanca Romero, P. M. Kowalski, G. Beridze, H. Schlenz, D. Bosbach, Performance of DFT+U method for prediction of structural and thermodynamic parameters of monazite-type ceramics. *J. Comput. Chem.* **35**, 1339–1346 (2014).
60. H. Jiang, P. Rinke, M. Scheffler, Electronic properties of lanthanide oxides from the GW perspective. *Phys. Rev. B.* **86**, 125115 (2012).

Acknowledgments: We thank A. J. Ehlmann for providing samples used in these studies. We thank J. Shamblin and M. McDonnell for thoughtful discussions regarding analysis of these

data. We thank M. Everett for guidance during the neutron scattering experiments. **Funding:** This work was supported by the U.S. Department of Energy (DOE), Office of Science, Basic Energy Sciences, under award DE-SC0020321. E.C.O. acknowledges support from the U.S. DOE, Office of Science, Office of Workforce Development for Teachers and Scientists, and Office of Science Graduate Student Research (SCGSR) program. The SCGSR program is administered by the Oak Ridge Institute for Science and Education for the DOE under contract number DE-SC0014664. D.D. acknowledges support from the Integrated University Program Graduate Fellowship program. The research at ORNL's Spallation Neutron Source was sponsored by the Scientific User Facilities Division, Office of Basic Energy Sciences, U.S. DOE. This research used the x-ray powder diffraction beamline of the National Synchrotron Light Source II, a U.S. DOE Office of Science User Facility operated for the DOE Office of Science by Brookhaven National Laboratory under contract no. DE-SC0012704. **Author contributions:** E.C.O. and M.K.L. conceived and designed the study. A.F.F. provided samples for the study. E.C.O., J.C.N., M.G.T., D.D., and M.K.L. performed the neutron scattering experiments and analyzed the data. G.B. performed the first principles calculations. E.C.O., K.E.S., R.C.E., G.B., A.F.F., and M.K.L. interpreted the data. E.C.O. drafted the manuscript with input from and critical review by all authors. **Competing interests:** The authors declare that they have no competing interests. **Data and materials availability:** All data needed to evaluate the conclusions in the paper are present in the paper and/or the Supplementary Materials. Additional data related to this paper may be requested from the authors.

Submitted 15 April 2020

Accepted 14 July 2020

Published 28 August 2020

10.1126/sciadv.abc2758

Citation: E. C. O'Quinn, K. E. Sickafus, R. C. Ewing, G. Baldinozzi, J. C. Neufeind, M. G. Tucker, A. F. Fuentes, D. Drey, M. K. Lang, Predicting short-range order and correlated phenomena in disordered crystalline materials. *Sci. Adv.* **6**, eabc2758 (2020).

Predicting short-range order and correlated phenomena in disordered crystalline materials

Eric C. O'Quinn, Kurt E. Sickafus, Rodney C. Ewing, Gianguido Baldinozzi, Joerg C. Neuefeind, Matthew G. Tucker, Antonio F. Fuentes, Devon Drey and Maik K. Lang

Sci Adv **6** (35), eabc2758.
DOI: 10.1126/sciadv.abc2758

ARTICLE TOOLS

<http://advances.sciencemag.org/content/6/35/eabc2758>

SUPPLEMENTARY MATERIALS

<http://advances.sciencemag.org/content/suppl/2020/08/24/6.35.eabc2758.DC1>

REFERENCES

This article cites 56 articles, 3 of which you can access for free
<http://advances.sciencemag.org/content/6/35/eabc2758#BIBL>

PERMISSIONS

<http://www.sciencemag.org/help/reprints-and-permissions>

Use of this article is subject to the [Terms of Service](#)

Science Advances (ISSN 2375-2548) is published by the American Association for the Advancement of Science, 1200 New York Avenue NW, Washington, DC 20005. The title *Science Advances* is a registered trademark of AAAS.

Copyright © 2020 The Authors, some rights reserved; exclusive licensee American Association for the Advancement of Science. No claim to original U.S. Government Works. Distributed under a Creative Commons Attribution NonCommercial License 4.0 (CC BY-NC).