Corner-, edge-, and facet-controlled growth of nanocrystals

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The ability to precisely control nanocrystal (NC) shape and composition is useful in many fields, including catalysis and plasmonics. Seed-mediated strategies have proven effective for preparing a wide variety of structures, but a poor understanding of how to selectively grow corners, edges, and facets has limited the development of a general strategy to control structure evolution. Here, we report a universal synthetic strategy for directing the site-specific growth of anisotropic seeds to prepare a library of designer nanostructures. This strategy leverages nucleation energy barrier profiles and the chemical potential of the growth solution to control the site-specific growth of NCs into exotic shapes and compositions. This strategy can be used to not only control where growth occurs on anisotropic seeds but also control the exposed facets of the newly grown regions. NCs of many shapes are synthesized, including over 10 here-to-fore never reported NCs and, in principle, many others are possible.

INTRODUCTION

Nanocrystal (NC) shape and composition are important parameters that influence the properties of such structures and, therefore, their uses in many fields, including catalysis (1–3), plasmonics (4, 5), therapeutics (6), and biological imaging (6, 7). Accordingly, a variety of methods have been developed that allow one to control these parameters, albeit in selected cases (8–11). The most prevalent methodologies involve seed-mediated syntheses. For example, capping agents have been used to selectively cap different faces of spherical seeds to promote anisotropic growth and the formation of nanocubes, octahedra, rhombic dodecahedra, and NCs of other shapes (12–15). Spherical gold and silver NCs have been used as plasmonic seeds, where light of a specific wavelength was used to guide the growth of triangular prisms with wavelength control over prism edge length (16, 17). In addition, underpotential deposition techniques have been used with gold and palladium seeds to prepare a wide variety of NC geometries, including rhombic dodecahedra, bipyramids, truncated ditetragonal prisms, and concave cubes (18–21).

While most studies have focused on spherical seeds, some anisotropic seeds have been used to prepare a variety of structures. For example, rod-shaped seeds have been used to generate elongated rhombic dodecahedral gold NCs (22). Moreover, rhombic dodecahedral gold seeds have been used as cores for the synthesis of Au–Ag core-shell NCs with cubic, cuboctahedral, and octahedral structures (23). Anisotropic seeds combined with masking or galvanic replacement have been used to prepare heterogeneous metallic or hollow nanostructures (24–26).

However, with most traditional seed-mediated approaches, the spherical or anisotropic seeds act as nuclei due to the absence of substantial energy barriers (E) for subsequent growth. Consequently, secondary nucleation does not occur, and instead, growth occurs at all positions on the seeds. Therefore, the development of a versatile strategy that allows one to control growth on seeds in a site-specific manner is a challenge yet to be addressed.

We reasoned that if we could introduce distinct E for secondary nucleation at different sites on an anisotropic seed, we would be able to achieve site-specific deposition by controlling the sites of secondary nucleation. If one analyzes the surface chemistry of a nonspherical seed, such as a triangular prism, one discovers that there are distinct E to additional growth due to differences in ligand density (caused by regions of different curvature; i.e., flat facets versus edges versus corners) and the exposed facet type (27–29). Therefore, we hypothesized that, through the use of appropriate ligands, substantial E differences on anisotropic seeds could be established, allowing one to access corner-, edge-, or facet-selective growth while tuning the supersaturation (Δµ) of the growth solution (the driving force) to only surmount certain E. In addition, further fine-tuning of Δµ would not only dictate the site of deposition (e.g., the edge or corner of an octahedron) but also determine the exposed facets (e.g., [100] or [111]) of the overgrown regions, thus controlling the overall shapes of the resulting NCs. Therefore, the ability to selectively grow additional material at specific sites on anisotropic seeds could be a general route for preparing a library of designer architectures with different shapes and compositions by following three fundamental design rules (curvature-selective, facet-selective, and specific exposed facet design rules).

RESULTS

The driving force for NC growth is the Δµ of the growth solution, which can be defined as the difference between chemical potential of the solute in solution (e.g., Au9 atoms) and that of the solid crystal (e.g., Au seed) (30). Growth only occurs at sites on anisotropic seeds when Δµ can surmount the nucleation E (i.e., Δµ > E). The E can be influenced by two factors—the curvature-dependent ligand distribution and the facet-dependent energy differences. We discuss below how Δµ and E can be independently tuned leading to site-specific nucleation and growth.

**Curvature-selective design rule: Sites with larger curvatures grow at lower Δµ**

Ligands tethered onto regions of different curvature on an anisotropic NC experience different degrees of confinement (28, 31), which...
ultimately translates into varying magnitudes of $E$ at different sites. For example, triangular gold nanoprism with different curvatures at corners (c), edges (e), and faces (f) are an excellent model system to investigate this premise. As shown in Fig. 1 (A to C), when the curvature (K) at a site is higher, the average distance between the ligands ($d$) is larger ($K_c > K_e > K_f$) such that $\delta_c > \delta_e > \delta_f$, which provides easier access to solutes for subsequent deposition and results in a lower $E$ for that site ($E_c < E_e < E_f$). Therefore, by adjusting the $\Delta\mu$ of the growth solution, specific curvature-selective energy windows can be attained, enabling corner- and edge-selective nucleation (Fig. 1A). Experimentally, we can tune $\Delta\mu$ of the growth solution by changing the reaction conditions. For example, increasing the concentration of the reducing agent ascorbic acid (AA), decreasing the reduction potential of the reduction agent, or decreasing the concentration of the ligand adsorbate hexadecyltrimethylammonium bromide (CTAB) all result in increased $\Delta\mu$ (detailed discussion in the Supplementary Materials).

To achieve selective growth, $E_c$, $E_e$, and $E_f$ must be well separated in magnitude. The length and binding affinity of the ligands are key parameters that affect the $E$ profiles and growth selectivity (see the Supplementary Materials for additional discussion). When a weakly binding ligand is used (e.g., CTAB), the $E$ values and their differences are negligible, resulting in uniform growth of the nanoprism into a larger nanoprism (Fig. S2). In other words, when only CTAB is used, secondary nucleation does not occur and growth selectivity cannot be achieved. We further studied ligands with higher binding affinities that can displace CTAB, including mPEG5k thiol and mPEG6 disulfide, such that CTAB in the following study is used only as a complexing agent to tune $\Delta\mu$ not $E$ (see note S1 for additional discussion) (32). However, when a relatively long ligand with a high binding affinity is used (e.g., mPEG5k thiol), the $E$ values of the nanoprism may exceed the homogeneous nucleation $E$, and growth is not observed on the nanoprism even when $\Delta\mu$ is higher than homogeneous nucleation $E$ (Fig. S2). We empirically found that mPEG6 disulfide results in the desired $E$ profiles, such that the $\Delta\mu-E$ relationship can be tuned to achieve corner-selective ($E_c < \Delta\mu < E_i$) and edge-selective ($E_e < \Delta\mu < E_i$) nucleation (Fig. 1D). Therefore, this ligand is used in all subsequent studies. Together, the curvature-selective design rule is that sites with larger K grow at lower $\Delta\mu$.

To test the generality of this curvature-selective design rule, NCs of various polyhedral shapes are used as seeds. Octahedral and concave rhombic dodecahedral gold seeds (Fig. 2, A and B) have corners and edges with different curvatures. Regardless of the polyhedral geometry of the seeds, subsequent site-specific gold deposition only on the corners (Fig. 2, D and E) or only the edges (Fig. 2, H and I) can be obtained by changing the AA concentration to tune the $\Delta\mu$ relative to $E$. When a seed NC has multiple types of corners (or edges) that are energetically nonequivalent, $\Delta\mu$ can be further tuned so that nucleation occurs preferentially at the lower- $E$ sites first. For example, in case of decahedral gold seeds (Fig. 2C) with two types of corners (a and b) and two types of edges (c and d) ($K_a > K_b > K_c > K_d$), four levels of continuous but independent control are possible over the selective growth on the different corners (Fig. 2, F and G) and edges (Fig. 2, J and K). Namely, we can successively grow (i) site a; (ii) sites a and b; (iii) sites a, b, and c; and (iv) sites a, b, c, and d.

**Facet-selective design rule: Facets with higher surface energies grow at lower $\Delta\mu$**

In addition to the curvature differences, facet energy ($\sigma$) differences also play an important role in influencing the corresponding $E$ profiles for subsequent NC nucleation. To decouple the effects of differing facets from that of curvature, the side faces of nanorods with no curvature difference, which are bound by alternating {100} and {110} facets (33), are used as a model system. The higher the $\sigma$ (resulting from the lower coordination number), the lower the $E$ (see the Supplementary Materials for detailed discussion) and the easier it is for solutes to access sites for subsequent nucleation. Therefore, by adjusting the $\Delta\mu-E$ relationship, specific facet-selective nucleation windows can be reached (Fig. 3A). Specifically, $\sigma_{[110]} > \sigma_{[100]}$ such that $E_{[100]} < E_{[110]}$. The $\Delta\mu$ and $E$ values for the octahedral, concave rhombic dodecahedral, and decahedral Au seed NCs, respectively. SEM images and models (insert top right) of (D to G) corner- and (H to K) edge-selective nucleation on the seed NC shown in the top row. Decahedral NCs (C) contain two types of corners (a and b) and two types of edges (c and d) due to curvature differences such that $K_a > K_b > K_c > K_d$, which results in four levels of continuous but independent control of selective nucleation as seen in (F), (G), (J), and (K). Scale bars, 100 nm.
$E_{[110]} < E_{[100]}$ (Fig. 3, B and C). Therefore, subsequent gold atoms were only selectively deposited on the four {110} facets of the nanorods’ side faces when $\Delta \mu$ only surmounts $E_{[110]}$ (Fig. 3, D and E). The selected area electron diffraction (SAED) patterns (Fig. 3, F and G) show that the newly grown parts are in the direction of the $<110>$ zone axis of the nanorods, while the parts in the orientation of the $<100>$ zone axis did not grow, thus confirming {110} facet-selective nucleation and growth. Together, the facet-selective design rule that emerges from this study is that facets with higher $\sigma$ grow at lower $\Delta \mu$.

The facet-selective design rule can also be generally applied to predict and tailor nanostructures when gold nanodisks are used as seeds (Fig. 3H). Gold nanodisks are synthesized by etching triangular nanoprisms, and the three areas of these nanodisks that used to be the prism corners have the same atomic arrangement as that of the original nanoprism corners. Along the edges of the nanodisks, the stacking fault of the twin plane causes {111} faces to form in alternating concave or convex orientations (Fig. 3I) (34). The concave structure creates a reentrant groove, a self-perpetuating ledge that increases the number of nearest neighbors for an adatom, increasing the stabilization energy, and greatly decreasing $E_{\text{concave}}$. However, on the convex side, an adatom attached to the surface has limited stabilization energy due to the presence of only three nearest neighbors, resulting in a higher $E_{\text{convex}}$ (Fig. 3). Therefore, deposition occurs exclusively on the concave-type facets when $E_{\text{concave}} < \Delta \mu < E_{\text{convex}}$ (Fig. 3L). SAED patterns (Fig. 3, M and N) indicate that the edges are grown in the same directions as the three original corners of the nanoprisms, thus suggesting concave-type facet-selective nucleation. Therefore, facet-selective nucleation that is not accessible using existing synthetic strategies can be achieved by taking advantage of facet-dependent energy differences coupled with $E$ profiles, which may provide an opportunity to design materials that could offer previously unknown fundamental insights and previously inaccessible functionalities.

**Specific exposed facet design rule: Facets with higher surface energies are exposed at higher $\Delta \mu$**

In addition to spatial control over nucleation, the $\Delta \mu-E$ relationship can be further tuned to control the exposed facets of the growth on the existing nuclei, thus programming the resulting shapes of the NCs. On the basis of the Thomson-Gibbs equation (32) in a growing crystal, facets with higher surface energies will appear when the $\Delta \mu$ of the growth solution is higher than that of {111} in light green (Fig. 4A). Therefore, using corner-nucleated octahedra as seeds (Fig. 4, B and E), growth occurs almost exclusively on the existing nuclei on the corners. The corners are bound by {111} facets at lower $\Delta \mu$ (100 mM CTAB) (Fig. 4, B and F), while the {100} facets begin to appear on the corners at higher $\Delta \mu$. 

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**Fig. 3. Facet-selective nucleation on the edges.** (A) Schematic of facet-selective growth on a Au nanorod, where growth can occur on (B) only the {110} facets of the seed NC by tuning $\Delta \mu$. (C) The idealized $E$ profile for NC growth is dictated by the facet’s energy, where $E_{[110]} < E_{[100]}$. SEM images of (D) Au nanorods and (E) {110} facet-selective growth on nanorods. Transmission electron microscopy (TEM) images and corresponding SAED patterns of nanorods with {110} facet-selective growth oriented along the (F) {100} and (G) {110} directions. (H) Schematic of concave-type facet-selective nucleation on Au nanodisks, where the concave-type facet-selective window can be reached by tuning $\Delta \mu$. (I) Side view of a Au nanodisk showing the concave- and convex-type facets. (J) Schematic showing the general trend of the $E$ profile of Au nanodisks, where $E_{\text{concave}} < E_{\text{convex}}$. SEM images of (K) Au nanodisks and (L) facet-selective grown nanodisks. TEM images and corresponding SAED patterns of (M) a Au nanoprism and (N) a Au nanodisk after concave-type facet-selective growth. The diffraction patterns in (M) and (N) are diagnostic of the [111] orientation. Scale bars, 100 nm.
(10 mM CTAB) (Fig. 4, B and G). Moreover, when edge-nucleated nanocubes are used as seeds (Fig. 4, C and I), subsequent growth only occurs on the existing nuclei along the edges. The edges are bound by {100} facets at higher $\Delta \mu$ (10 mM CTAB) (Fig. 4, C and J), while the {111} facets begin to appear along the edges at lower $\Delta \mu$ (100 mM CTAB) (Fig. 4, C and K, and fig. S8).

Furthermore, a broad library of structures with specific exposed facets can be obtained by controlling the concentration of the seeds in addition to $\Delta \mu$ (figs. S9 and S10). This exposed facet design rule can be applied to seeds of different shapes, such as gold concave rhombic dodecahedra and nanodisks (fig. S10, see the Supplementary Materials for a detailed discussion). These results not only confirm the design rule but also markedly increase the number and diversity of nanostructures that can be accessed using seed-mediated syntheses.

**General use of this strategy**

To further explore the generality of this strategy, gold NC seed growth was studied as a function of growth solution metal ion composition and reducing agent. Corner- or edge-selective growth of Ag or Pd onto Au NCs of different shapes, including nanoprisms, octahedra, and concave rhombic dodecahedra, can be similarly controlled (Fig. 5). Elemental mapping confirms the spatial arrangement of the NCs. Therefore, this strategy provides a way to expand the compositional library of NCs through crystal engineering via site-specific growth.

**DISCUSSION**

We have developed a new and versatile synthetic strategy, where curvature/facet-dependent $E$ and $\Delta \mu$-$E$ relationships are implemented for the first time to control site-specific growth on NCs. This strategy provides a different way of using seed-mediated NC syntheses to direct selective growth on anisotropic NC seeds by following curvature-selective, facet-selective, and specific exposed facet design rules. Although we only report proof-of-concept architectures of Au, Ag, and Pd here, the strategy presented is generalizable, and more sophisticated architectures with other compositional combinations likely can be synthesized. Given the enormous library of nanostructures that can be tailored by this universal strategy, this work advances the NC design field by allowing for greater structural complexity,
specificity, and compositional diversity. Such structures will positively affect a broad range of disciplines, spanning catalysis, plasmonics, magnetics, electronics, biology, and medicine.

**MATERIALS AND METHODS**

**Functionalization of anisotropic NCs**

Anisotropic NCs were functionalized with mPEG6 disulfide. One-milliliter aliquots of the as-synthesized NC solution were centrifuged for 6 min at 5000 to 10,000 rpm depending on the NC shape used. After the supernatant was removed, the NCs were resuspended in water and centrifuged a second time under the same centrifugation conditions as the first time. After removal of the supernatant, 900 μl of 1 μM mPEG6 disulfide and 100 μl of 1 weight % (wt %) SDS were added directly to the pellet. The NC solution was placed on a shaker at 1000 rpm for 1 day. To remove excess mPEG6 disulfide, the NC solution was centrifuged three times with the supernatant removed each time, and then the NCs were resuspended in 0.1 wt % SDS after the first two centrifugation steps and in 10 mM CTAB after the third centrifugation step. All the functionalized NCs used as seeds for the following experiments were at a 10 optical density (OD) concentration.

**Corner/edge-selective growth**

The functionalized NCs were used as seeds for subsequent growth with different AA and CTAB concentrations. Typically, for corner- and edge-selective growth, 6.24 μl of 25 mM HAuCl₄ was added into 1.25 ml of 10 mM CTAB solution, and then 100 mM AA (for corner-selective growth, 2 to 3 μl; for edge-selective growth, 10 to 11 μl depending on different shapes of seeds) was added. The solution was mixed by vortexing for 10 s. Next, 60 μl of seeds was injected immediately followed by vortexing for 10 s. After allowing 4 hours for completion of NC growth, the reaction mixture was purified from excess reagents by centrifugation (5 min at 5000 to 10,000 rpm depending on shapes of different seeds). The supernatant was removed, and the NCs were resuspended in 1.0 ml of 1 mM CTAB by brief sonication (~10 s).

**Facet-selective growth**

For nanorods, 1.25 ml of 10 mM CTAB, 6.24 μl of 25 mM HAuCl₄, and 15 μl of 100 mM AA were mixed. Then, 60 μl of seeds was injected, and the solution was allowed to react for 4 hours. Moreover, for nanodisks, 1.25 ml of 10 mM CTAB, 6.24 μl of 25 mM HAuCl₄, and 2.5 μl of 100 mM AA were mixed. Then, 30 μl of seeds was injected, and the solution was allowed to react for 6 hours.

**Exposed facet control**

The concentration of CTAB was adjusted to produce site-specifically grown NCs with different types of exposed facets (with the other reaction conditions the same as in the case of the corner/edge-selective growth of NCs). Ten mM CTAB was used to synthesize grown NCs bound by high-energy surfaces, while 100 mM CTAB was used for low-energy surfaces. The amount of deposition was increased by decreasing the amount of seeds from 60 to 6 μl.

**Synthesis of heterogeneous NCs**

Synthesis of Au/Pd NCs: 60 μl of seeds was added to 1.25 ml of 10 mM CTAB solution containing 15.6 μl of 10 mM AgNO₃. Afterward, 1 M NaOH (for corner selective growth, 7.5 μl; for edge selective growth, 10 μl) was introduced. After thorough mixing, 75 μl of 100 mM AA was finally injected, immediately followed by 10 s of vortexing. The solution was kept at room temperature overnight. NaOH was used here to increase the pH of the growth solution, which decreased the reduction potential of AA and thus increased Δν of the growth solution.

Synthesis of Au/Pd NCs: 10 mM H₂PdCl₄ aqueous solution was prepared by completely dissolving 89 mg of PdCl₂ in 50 ml of 20 mM HCl in a boiling water bath. A total of 1.25 ml of 10 mM CTAB, 60 μl of seeds, and 15.6 μl of 10 mM H₂PdCl₄ were mixed. Then, 15 μl of 100 mM AA was injected, and the solution was allowed to react overnight.

**SUPPLEMENTARY MATERIALS**

Supplementary material for this article is available at http://advances.sciencemag.org/cgi/content/full/7/3/eabf1410/DC1

**REFERENCES AND NOTES**


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