Introduction

The COVID-19 pandemic is a devastating historical event which is currently impacting nearly all of mankind. SARS-CoV-2 incidence is surging in numerous cities and countries across the globe (1), and infection carries a high mortality rate, particularly among the elderly (2–4). While social distancing has slowed and even eliminated many local epidemics (5), it is not an economically viable long-term strategy. There is no evidence of widespread herd immunity and a vaccine is unlikely to be developed and widely implemented within the next 6 months. Therefore, second and third waves of infection are likely to occur over the next two years (6).

It is imperative that optimal treatment strategies of COVID-19 are identified urgently to ensure that the case fatality rate is lower during subsequent local epidemics. To date, selection of antiviral agents has been empirical and guided by limited or absent data. While clinical trials are being fast-tracked to identify therapeutics that lower hospitalization and death rates, the planning phase for these trials is narrow. Therefore, effective tools are urgently needed to optimize clinical trial design and selection of therapeutic agents.

Here we use mathematical models to project the possible impact of two small molecular agents, remdesivir and selinexor; as well as broadly neutralizing antibodies and cellular immunotherapies. The goal of our models is to interpret emerging clinical trial data, and in turn to perfect subsequent trials in terms of selection of antiviral agents, timing of therapy, dosage, treatment duration, avoidance of drug resistance and selection of virologic endpoints. Overall, our simulations support initiation of therapy soon after symptoms develop and also suggest the urgent need for studies to identify virologic surrogates of SARS-CoV-2 severity.

Results

SARS-CoV-2 natural history

We used four datasets of SARS-CoV-2 shedding in the absence of effective treatment to develop and validate a mathematical model. This data included 25 infected people: 11 from Singapore (7), 9 from Germany (8), one from South Korea (9), and 4 from France (10) (Fig. 1). Notably, sampling techniques differed across studies. In Singapore, South Korea and France, samples were obtained with nasopharyngeal swabs, whereas in Germany viral loads were measured directly from sputum. Shedding was notable for an early peak, followed by three phases of viral decay including a rapid initial decline from peak, a slower period of decay of variable length, and a final abrupt viral elimination phase. Of note, we only captured the viral peak as well as the final rapid clearance phase in a subset of study participants.

SARS-CoV-2 mathematical model

We developed a series of ordinary differential equations to fit
to the viral load data (Fig. 1a, Methods and Materials). The equations capture the coupled interactions of susceptible cells, infected cells, SARS-CoV-2 and a mounting immune response. In keeping with the standard viral dynamics model (11, 12), virus enters susceptible cells and converts them to infected cells which then produce virus at a fixed rate. The virus induces a cytopathic effect on infected cells even in the absence of immunity.

An early innate immune response and a late acquired immune response are known to be vital for clearance of SARS and MERS virus infections (13). In keeping with these observations, when we simulated our model without innate and acquired immune terms (thereby limiting the mechanism of viral elimination to target cell limitation), model fit to the data was spoor. We therefore added a two-stage immune response. The first stage accounts for the rate of infected cell elimination by the innate immune system and is governed by an exponent in the infected cell death rate term; in accordance with prior models, we refer to this as the density-dependent immune response (14, 15). The second phase represents a slower acquired cytolytic response in which the per cell killing rate saturates once the number of effector cells exceeds a certain level. We model this with stages of presumed effector cell precursors which differentiate at rate $q$ as a method to calibrate timing of this response (Methods).

Our model reproduced viral load kinetics in all 25 participants (Fig. 1b). In certain cases, the model only fit to available data from the later stages of shedding, whereas it recapitulated the entirety of viral expansion, peak and decelerating clearance for the several study participants with available early data (S5, S14, S18, G1, G2, G5, G7). In keeping with observations from a recent clinical trial (16), low level shedding continued past 20 days for 8/25 participants (S3, S6, G1, G2, G3, G5, G6, G7), whereas viral elimination occurred earlier in the remaining infected people.

The component of the late acquired immune response responsible for elimination of infection remains unknown. Virus-specific antibodies (17, 18), as well as virus-specific CD4+ and CD8+ T cell responses (19–22), are noted as soon as a week after infection. To account for the fact that humoral immunity may be clearing infection, we also constructed a model in which neutralizing antibodies lower viral infectivity in a density dependent manner (Methods). In this model, infectivity rate saturates once the total number of antibodies exceeds a certain level. We achieved equal fit to the data whether we assumed a cytolytic T-cell mediated response (Fig. 1b) or a neutralizing antibody response (Fig. S1). We are therefore unable to identify which mechanism is responsible for late clearance of virus, though both models provide the same output with simulation of therapies.

While both models allow equivalent viral kinetics, for several reasons we selected the cytolytic immune model for our therapy modeling. First, depletion of virus specific T cells abrogates control of SARS in mice (23, 24); interferon signaling to T cells is vital to elimination of both MERS and SARS (25). Second, severe SARS-CoV-2 is observed in solid organ transplantation patients on T cell suppressing therapies (26). Third, impaired T cell function is the primary risk factor for severe lung manifestations of nearly all other respiratory viruses (27, 28). Finally, T cells play a vital role in mediating cytokine storm and acute respiratory distress syndrome following SARS (29, 30): the intensity of the cytokine response is projected indirectly in our model based on quantification of the cytolytic response.

**Timing and intensity of innate and acquired cytolytic responses**

We continuously quantified the value of the immune terms in all 25 participants: the per cell killing rate and total number of cells killed per day was extremely high during the first several days of infection in all participants (Fig. 2a, b), coinciding with peak viral load. The acquired cytolytic immune response initiated at various timepoints across participants (day 5-14) and led to similar contemporaneous per cell killing rates to innate immune responses, but much lower numbers of total cells killed per day relative to the innate response at peak viral load (Fig. 2b), but was sufficient and necessary to eliminate remaining infection (Fig. 1b).

**Remdesivir pharmacokinetics and pharmacodynamics**

We developed a pharmacokinetic / pharmacodynamic (PK/PD) model of remdesivir (Fig. 3a), a broad-spectrum nucleotide analog that targets SARS-CoV-2 replication in infected cells (31). The model links intravenous administration with plasma levels of free drug and concentrations of the drug’s active nucleotide-triphosphate component (NTP) observed within PBMCs in non-human primates (32), and captures the slow decay of NTP within this compartment (Fig. 3b). With multiple doses, we project fluctuating levels of NTP in target cells over time (Fig. 3c) followed by somewhat protracted decay after cessation of treatment.

We next simulated possible dose response curves of antiviral efficacy, which capture the percentage of viral replication eliminated, according to micromolar concentration of drug. The percent of viral replication suppression at a given intracellular drug concentration is dependent on the intracellular EC$_{50}$ of the drug, or the concentration of drug required to lower viral replication by 50% (Fig. 3d). Of note the intracellular EC$_{50}$ is unknown for remdesivir, particularly in vivo, making precise predictions of clinical trial outcomes impossible.

Finally, we combined the PK and PD models as in Fig. 3a to project the percentage of viral replication inhibited over time at different assumed intracellular EC$_{50}$ values (33, 34).
With high assumed drug potency (EC₅₀=0.8 uM), antiviral effects are sustained over the 10-day dosing interval and maintained for several days after drug delivery has stopped (Fig. 3e). At higher assumed EC₅₀ values, remdesivir potency is projected to be lower.

**Projections of SARS-CoV-2 outcomes assuming remdesivir treatment during early and late symptomatic phases**

We next simulated therapy at day 10 of infection (Fig. 4a) when severely infected people often seek hospital care, and at day 5 of infection immediately after viral peak (Fig. 4b) when infected people often become symptomatic. In both cases, when remdesivir in vivo potency was assumed to be high (EC₅₀=0.8 uM), viral elimination occurred rapidly after initiation of therapy. This effect occurred because of unopposed removal of approximately 100-10,000 infected cells per day by an ongoing innate immune response (Fig. 2b).

Simulations with the assumption of a less potent version of remdesivir (EC₅₀= 8 or 80 uM) resulted in a lower viral clearance slope. This result implies that viral clearance slope in clinical trials can be used in concert with our model to directly estimate the in vivo intracellular EC₅₀ value of remdesivir in each treated patient. The model can then be used to project the effect of increasing or decreasing doses in subsequent trials (34).

**Projections of SARS-CoV-2 outcomes assuming extremely early remdesivir treatment during the pre-symptomatic phase**

We next performed simulations of therapy at very early timepoints during infection at and prior to peak viral load. Most infected people are pre-symptomatic at this stage so these model realizations may most closely reflect implementation of a post exposure prophylaxis (PEP) strategy in which these model realizations may most closely reflect implementation of a post exposure prophylaxis (PEP) strategy in which the in vivo potency of remdesivir against SARS-CoV-2 in humans is unknown, as well as infection duration at the time of treatment initiation. As dependent variables, we selected shedding duration and viral area under the curve (AUC) because it is unclear which of these outcomes is a stronger predictor of progression to cytokine storm and respiratory failure, as well as transmissibility, in infected people. We also included the final tally of effector cells as this outcome may also be predictive of likelihood of cytokine storm (36).

Early initiation of a highly potent therapy was predictive of lower shedding duration whether given in the pre-peak asymptomatic phase or in the post-peak symptomatic phase beyond day 2-4 of infection. However, extremely early initiation of a lower potency therapy was predicted to prolong shedding relative to no treatment (Fig. 5a), due to insufficient early immunity against the virus and the lack of depletion of susceptible cells.

Both high drug potency and extremely early treatment initiation during the pre-symptomatic stage of infection were required to significantly lower viral AUC. Even highly potent therapy during the earliest symptomatic phase at days 4-5 had only a slight impact on AUC, reflecting the fact that most virus and infected cells are generated during the first 2-3 days of productive SARS-CoV-2 infection (35) (Fig. 5b).

Finally, initiation of a highly potent therapy within 6 days of infection lowered the extent of the effector cell response in our simulations by a full order of magnitude (Fig. 5c) which suggests that an early treatment strategy could lower deleterious infection associated inflammation.

**Theoretical kinetics of drug resistant variants**

Based on the mutation rate of positive ssRNA viruses of approximately 10⁻² mutations per base pair per cell infection (37), and on the fact that two separate mutations may induce partial remdesivir resistance in SARS which in turn leads to a less fit virus (38), we explored the theoretical possibility that a drug resistant mutant could emerge during treatment. Under this hypothesis, we then estimated the probability that...
a drug resistant mutant would emerge during therapy. When we assumed a potent therapy (EC_{50}=0.8), the model projects that while single and double mutants emerge, they remain sub-dominant and do not meaningfully extend duration of shedding if dosed during the symptomatic phase of disease, though resistant strains may emerge and even predominate with early dosing (Fig. 6 a,b). However, if only moderate potency is assumed, then a single mutant with resistance is predicted to possibly induce more prolonged shedding, particularly if therapy is initiated before or during viral peak (Fig. 7 a,b).

If we assume that a single point mutation in SARS-CoV-2 could theoretically induce complete drug resistance, then treatment failure may occur regardless of dosage timing. The resistant strain is predicted to predominate raising the possibility of transmitted drug resistance (Fig. S3).

**Selinexor treatment predictions**

Following SARS-CoV-2 infection and the nuclear import of viral genetic material at the cellular level, the nucleocyttoplasmic export of viral proteins is essential for efficient viral replication mediated by exportin-1 (XPO1). Selinexor is a selective inhibitor of this key step of the late-stage assembly processes (39). Selinexor has been demonstrated to have dose-dependent activity against SARS-CoV-2 replication. Selinexor is currently being tested in human clinical trials for COVID-19 treatment (40).

Using a multi-compartment PK/PD model for selinexor (Fig. 8a), we first recapitulated plasma parent drug levels over time following a single dose (41) (Fig. 8b), PBMC drug levels under different assumptions of drug absorption (Fig. 8c), and compensatory XPO1 mRNA expression following dosing (Fig. 8d). We then simulated plasma and PBMC drug levels (assuming low and high estimates for drug absorption) with three times weekly doses over 4 weeks (Fig. 8e) as proposed in the clinical trial (https://clinicaltrials.gov/ct2/show/NCT04349098?term=selinexor&draw=3&rank=14). After generating theoretical dose response curves with different assumptions for in vivo EC_{50} (Fig. 8f), we projected compensatory XPO1 mRNA expression (Fig. 8 g) and drug efficacy over time (Fig. 8h).

As with remdesivir, the predicted efficacy of therapy on viral shedding depended on the timing of treatment and the intracellular in vivo EC_{50} (Fig. S4a-d). Lower shedding duration occurred with earlier timing of therapy. Lower viral AUC again required extremely early initiation of potent treatment (Fig. S4d). The model again predicted the possibility of prolonged shedding with sub-potent early initiation of therapy (Fig. S4d).

**Broadly neutralizing antibody predictions**

We next simulated a single infusion of hypothetical broadly neutralizing antibodies with prolonged half-life. Broadly neutralizing antibodies are designed to stop infection of new cells rather than eliminate viral replication. We used a dual compartment PK model (Fig. 9a), estimated antibody levels over time following a single dose (Fig. 9b), generated theoretical dose response curves (Fig. 9c), and then projected antibody efficacy over time (Fig. 9d). The predicted efficacy of therapy on shedding again was dependent on timing of treatment and the in vivo EC_{50} (Fig. S5a-d). Once again, to lower duration of shedding and the number of effector cells depended on therapeutic potency, while effective lowering of viral AUC required extremely early initiation of potent treatment (Fig. S5e-g).

**Immunotherapy predictions**

As natural killer cells-based treatments are being developed and studied for COVID-19 (https://clinicaltrials.gov/ct2/show/NCT04280224), we generalized the potential hypothetical effects of a cellular immunotherapy which would presumably decrease the lifespan of infected cells. We projected that such an intervention would need to increase this rate 10-fold to match the efficacy of a potent small molecular agent (Fig. 10a-c). Immunotherapies were projected to have limited efficacy if started prior to peak shedding (Fig. 10d).

**Discussion**

SARS-CoV-2 infection is characterized by a stereotypical viral kinetic pattern with a high peak viral load during the first several days of infection, a subsequent short rapid decay period followed by a slower clearance phase of variable duration, and finally rapid elimination phase. Our mathematical model reproduces this data and explains that the transition from first to second phase viral decay is governed by a density dependent term in which a massive die off of infected cells occurs during peak viremia, as well as target cell elimination. Because an acquired immune response would continue to intensify rather than subside even after viral loads lower, we attribute the density-dependent term to innate mechanisms. Our results suggest that this early response results in the quick elimination of millions of infected cells.

Viral clearance rate slows considerably once the viral load decreases below a threshold of ~10^5 RNA copies. A late slowly expanding acquired immune response is predicted to induce eradication of infected cells in the upper airway 2-20 days later. The timing of this final response appears to be variable among infected people in accordance with heterogeneous shedding duration during COVID-19 infection (42). Moreover, it is unknown if cessation of viral replication in the nasopharynx guarantees the same result in the lung or other anatomic compartments (8). Indeed, viral dynamics under therapy differ dramatically within the nasal passage and lung.
in a rhesus macaque model of remdesivir treatment for COVID-19 (43).

We are not able to differentiate whether neutralizing antibodies or cytolytic T cells are responsible for late clearance of infection, as both modeling approaches allow excellent model fitting to the data. Based on the fact that normal T cell function is a prerequisite for the rapid clearance of other viral infections, including SARS and MERS (24, 25), and because excess T cell responses may contribute to cytokine storm and ARDS (30), we elected to assume that T cells govern elimination of infected cells. However, our therapeutic model generates equivalent outcomes whether we assume cell-mediated or humoral viral elimination.

We simulated antiviral therapies on top of our natural history model to shed light on the possible impact of the timing and potency of antiviral therapies on outcomes. While accurate prediction is impossible in the absence of clinical trial data, our observations highlight the importance of considering off-treatment viral dynamics in order to understand treatment effects. Our results can guide future study design and assist in interpretation of forthcoming trial data in multiple ways.

First, it is critical to know whether in vitro potency assessments of remdesivir, selinexor and bNAbs can be projected onto human infection. We previously demonstrated that in vivo EC50 values for antiviral agents can exceed estimates derived from cell cultures experiments by a multiple of 5-10 (34). A similar observation has been hypothesized for HIV targeting monoclonal neutralizing antibodies (44). It is unclear if this discrepancy occurs due to low blood levels in tissue, different cell metabolism of drug in tissue or higher protein binding in vivo. Whatever the case, if in vitro potency measurements of selinexor and remdesivir overestimate in vivo activity, or if higher intracellular levels are required than in plasma, then these drugs may be less effective in clinical trials. Higher dosing may be a necessary solution to circumvent this issue.

Second, effective dosing after symptom development predicts rapid subsequent elimination of infected cells. Most current clinical trials are focused primarily on hospitalized patients whereas our results and those from other COVID-19 models suggest that treatment in the days immediately following symptom onset will decrease the duration of detectable viral shedding (45, 46). Our model also predicts that early treatment (before viral peak, usually <5 days post-infection) will limit the extent of the cytolytic immune response required to clear infection. If either of these outcomes are correlates of progression to severe disease as appears to be the case clinically (47), and transmission risk, then as with HIV (48), influenza (49), and Ebola (50), early test and treat is a vital, currently overlooked strategy.

Third, effective dosing soon after onset of symptoms (usually post-peak and >5 days post-infection) is predicted to have a less significant effect on viral load AUC. This phenomenon occurs because the amount of virus produced per hour at the early peak is far higher than the amount produced per day during the lower viral load second decay phase. This finding provides a cautionary message: if subsequent disease severity and development is imprinted during the high viral load, pre-symptomatic acute phase of infection, then early antiviral therapy could theoretically eliminate further shedding without altering clinical outcomes. Moreover, if extremely high viral load periods are responsible for most transmissions as suggested by the median 5-day serial interval of infection (51), then early elimination of shedding may not significantly lower transmissibility either. Overall this result highlights the urgent need for studies which identify early viral and immune correlates of severe disease and transmissibility. Preliminary studies suggest that presenting viral load may impact disease severity (52) but are not discriminated by viral AU and are also potentially biased by variable timing of samples.

Fourth, if therapy is initiated during the pre-symptomatic stage of infection (usually <5 days post-infection and most likely to be captured during PEP trials (53)), then the outcomes of the clinical trial is predicated on the potency of antiviral therapy. Subtherapeutic treatments may even prolong infection by blocking adequate triggering of innate immunity, total depletion of susceptible cells and thus, such therapies may be predisposed to drug resistance. Of note, our model’s predictions differ in this respect from those derived from other existing intra-host models of SARS-CoV-2 that do not emphasize the role of the immune response in eliminating infected cells (45, 46). Based on these different projections, we suggest sampling at late timepoints during post exposure prophylaxis trials. While we emphasize that our model’s projections of higher late viral loads following subpotent extremely treatment are uncertain based on limited knowledge of thresholds required for induction of effective acquired immune response, it is nevertheless notable that this outcome has been observed in the nasal passages of remdesivir treated rhesus macaques (43).

Fifth, our hypothetical approach suggests that while emergence of low-level drug resistant strains may occur commonly during COVID-19 treatment with remdesivir, this is unlikely to predispose to treatment failure provided the drug is potent against the predominant susceptible strain. Resistant variants may be present at low levels relative to susceptible strains making transmission of resistance less likely. Important exceptions may occur in immunocompromised hosts who might shed respiratory viruses for longer and at higher levels, thereby increasing the chance of de novo resistance (54), or in the context of only moderately potent antiviral therapy. Of note, these hypotheses are relevant and
require experimental validation.

Finally, our model projects a high likelihood of success for neutralizing antibodies and cellular immunotherapies provided that they achieve adequate potency and are dosed soon after development of symptoms.

Our model has important limitations. Most critically, it cannot be used to predict trial outcomes but rather establishes important principles to consider when designing and interpreting trials. We also do not frequently capture viral expansion during the first few days of SARS-CoV-2 infection: while parameter values for viral infectivity and replication rate may vary across infected people, the limited amount of early infection data prevents us from identifying the degree of variance in these parameters. Similarly, we lack adequate resistance data on all of our simulated therapies.

In summary, our model provides a broad platform for assessment of all major types of therapies. Our results demonstrate the need to differentiate whether duration of viral shedding or viral AUC is the more relevant surrogate of COVID-19 severity. If AUC is most predictive of poor outcomes, then all forms of antiviral therapy outside of potent PEP are unlikely to provide clinical benefit. However, if shedding duration is the best surrogate, then an early test and treat approach is highly promising for limiting the likelihood of severe disease.

Materials and Methods

Study design

We employed ordinary differential equation models to analyze the in-host SARS-CoV-2 dynamics in infected individuals and the potential in vivo effect of different treatment strategies. First, we fit models to the viral load data from different sources using a nonlinear-mixed effects approach. Second, we used pharmacokinetics models to fit observed plasma concentration of remdesivir (RDV) and its active nucleoside triphosphate form in PBMCs, and blood and PBMC concentrations of selinexor. Third, we simulated dose response curves for antiviral effect of RDV and selinexor using different possible half maximal effective concentration (EC50) based on in-vitro estimations against SARS-CoV-2. Fourth, we simulated therapy at different times during infection to analyze the potential reduction of SARS-CoV-2 shedding. Finally, we repeated projections of therapy including the emergence of resistance to therapy.

SARS-CoV-2 viral load data

We analyzed viral load data from persons infected with SARS-CoV-2 who were monitored and received supported therapy in hospitals in Singapore (n=11), Germany (n=9), South Korea (n=1), and France (n=4). Persons who had less than 4 data points or had oscillatory viral dynamics were excluded. These data are all published prior to our analysis.

The first data set was obtained from SARS-CoV-2-infected patients followed at 4 hospitals in Singapore from January 23rd to February 23rd, 2020 (7). All patients had travelled from Wuhan, China in the two weeks before enrollment. Viral load observations were obtained from different specimens (blood, stool, and urine samples), but we analyzed those coming from nasopharyngeal swabs. Cycle threshold were obtained with reverse transcriptase polymerase chain reaction (RT-PCR) at multiple times during the first 2 weeks after enrollment.

The second data set was obtained from infected patients enrolled and treated in a single hospital in Munich, Germany from January 23rd to January 27th, 2020 (8). For all patients, the infection was reported to happen after contact with an index case. Viral load observations were obtained daily from sputum, pharyngeal swabs and stool using RT-PCR. We analyzed viral RNA concentrations from sputum.

The third data set was from the first SARS-CoV-2 infected case in South Korea, a 35-year-old Chinese citizen coming from Wuhan, China (9). Nasopharyngeal swabs viral loads were obtained daily from day 2 of symptoms onset using RT-PCR.

The fourth data set came from 4 patients admitted to hospitals in Paris or Bordeaux, France with viral loads obtained from nasopharyngeal swabs using RT-PCR (10). We analyzed viral load data digitized from the published study.

When viral load observations were only published in cycle threshold (Ct) values we converted them to copies per swab using the relation values in (55). We assumed a lower limit of detection of 100 copies per sample.

Pharmacokinetic data

PK data of RDV was gathered from (32), where non-Human Primates (NHPs) intravenously received RDV at 10mg/kg dose at day 0 and the plasma concentration of RDV and its active nucleoside triphosphate form in PBMCs were recorded over 24 hours. We digitize this data and employed it to fit our PK model of RDV. PK selinexor data was gathered from (41) for model fitting.

Mathematical modeling of SARS-COV-2 dynamics

To understand the observed SARS-CoV-2 shedding dynamics we developed a viral infection model modifying previous models of virus dynamics (11, 12, 56). In this model, susceptible cells (S) are infected at rate $\beta VS$ by SARS-CoV-2 (V). SARS-CoV-2-infected cells (I) are cleared in two ways: (1) by an innate response with density dependent rate $\delta I_k$ (14, 15); and (2) an acquired response with rate $\frac{me^r}{e^{rt}+f^r}$ mediated by SARS-CoV-2-specific effector cells (E). The exponent $k$ describes by how much the first death rate depends on the infected cell density. The Hill coefficient $r$ parameterizes the nonlinearity of the second response and allows for rapid
saturation of the killing. Parameter $\phi$ defines the effector cell level by which killing of infected cells by $E$ is half maximal. SARS-Co-V-2 is produced at a rate $\pi$ and cleared with rate $\gamma$. In the model, SARS-Co-V-2-specific effector cells rise after $n$ stages from precursors cells ($M_{i=1...n}$). The first precursor cell compartment ($M_1$) proliferates in the presence of infection with rate $\omega M_1$ and differentiates into the effector cell at a per capita rate $\delta E$. The best instance of the model is expressed as a schematic (Fig. 1a) and here as a system of ordinary differential equations:

\[
\begin{align*}
\frac{dS}{dt} &= -\beta VS \\
\frac{dI}{dt} &= \beta VS - \delta I^k I - m \frac{E^r}{E^r + \phi^r} - I \\
\frac{dV}{dt} &= \pi I - \gamma V \\
\frac{dM_1}{dt} &= \omega M_1 - q M_1 \\
\frac{dM_{i=2...n}}{dt} &= q(M_{i-1} - M_i) \\
\frac{dE}{dt} &= q M_n - \delta E
\end{align*}
\]

The neutralizing antibody model in Fig S1 is equivalent to the neutralizing antibody model in (57) (See Table S1). Briefly, we obtained a maximum likelihood estimation of the population median (fixed parameters, random effects were specified, and the standard deviation of the killing. Parameter $\phi$ defines the effector cell level by which killing of infected cells by $E$ is half maximal. SARS-Co-V-2 is produced at a rate $\pi$ and cleared with rate $\gamma$. In the model, SARS-Co-V-2-specific effector cells rise after $n$ stages from precursors cells ($M_{i=1...n}$). The first precursor cell compartment ($M_1$) proliferates in the presence of infection with rate $\omega M_1$ and differentiates into the effector cell at a per capita rate $\delta E$. The best instance of the model is expressed as a schematic (Fig. 1a) and here as a system of ordinary differential equations:

\[
\begin{align*}
\frac{dS}{dt} &= -\beta VS \\
\frac{dI}{dt} &= \beta VS - \delta I^k I - m \frac{E^r}{E^r + \phi^r} - I \\
\frac{dV}{dt} &= \pi I - \gamma V \\
\frac{dM_1}{dt} &= \omega M_1 - q M_1 \\
\frac{dM_{i=2...n}}{dt} &= q(M_{i-1} - M_i) \\
\frac{dE}{dt} &= q M_n - \delta E
\end{align*}
\]

The neutralizing antibody model in Fig S1 is equivalent to the neutralizing antibody model in (57) (See Table S1). Briefly, we obtained a maximum likelihood estimation of the population median (fixed parameters, random effects were specified, and the standard deviation of the killing. Parameter $\phi$ defines the effector cell level by which killing of infected cells by $E$ is half maximal. SARS-Co-V-2 is produced at a rate $\pi$ and cleared with rate $\gamma$. In the model, SARS-Co-V-2-specific effector cells rise after $n$ stages from precursors cells ($M_{i=1...n}$). The first precursor cell compartment ($M_1$) proliferates in the presence of infection with rate $\omega M_1$ and differentiates into the effector cell at a per capita rate $\delta E$. The best instance of the model is expressed as a schematic (Fig. 1a) and here as a system of ordinary differential equations:

\[
\begin{align*}
\frac{dS}{dt} &= -\beta VS \\
\frac{dI}{dt} &= \beta VS - \delta I^k I - m \frac{E^r}{E^r + \phi^r} - I \\
\frac{dV}{dt} &= \pi I - \gamma V \\
\frac{dM_1}{dt} &= \omega M_1 - q M_1 \\
\frac{dM_{i=2...n}}{dt} &= q(M_{i-1} - M_i) \\
\frac{dE}{dt} &= q M_n - \delta E
\end{align*}
\]

To reproduce the PK data of RDV, we employed a simple two compartment model where the first compartment represents the amount of RDV in plasma ($C_P$, volume $V_P$) and the second compartment denotes the amount of its active nucleoside triphosphate form in PBMCs ($C_a$, volume $V_a$). Here, we assume that RDV gets metabolized to its active nucleoside triphosphate form at rate $k_{pa}$ whereas RDV and its active nucleoside triphosphate form are eliminated from their respective compartments at rates $k_c$ and $k_a$, respectively. The model is given by,

\[
\begin{align*}
\frac{dC_P}{dt} &= -k_{pa} C_P - k_c C_P \\
\frac{dC_a}{dt} &= k_{pa} C_P - k_a C_a
\end{align*}
\]

As the drug concentration was recorded in $\mu$M, we convert the amount of the drug given in mg to $\mu$M by dividing $C_P$ and $C_a$ by conversion factors $V_1$ and $V_2$, respectively. Here, $V_1$ and $V_2$ are a combination of the volume of the distribution of two compartments ($V_P$ and $V_a$) and the molar mass of two forms of RDV ($M_P$ and $M_a$). The relationship follows, $V_1 = \frac{V_P M_P}{10^3}$ and $V_2 = \frac{V_a M_a}{10^3}$.

We fit this model to the PK data from NHP (32), using a non-linear least squares approach using an initial dose of 10mg/kg. We adapted the dose in humans (200mg and 100mg) assuming a normal weight of 70kg.

**Pharmacokinetic modeling of selenexor**

We used a two-compartment model of therapy for selenexor during the observed data.

For each model fit we assumed $t = 0$ as the time of first positive viral load for each person. However, we defined the initial value as the time of infection, i.e., when $I(t_{init}) = 1$ cell. Since infection starts before the first detected viral load, we have that $t_{init} < 0$. We fixed other initial values as $S(t_{init}) = 10^7$ cells, $V(t_{init}) = \frac{\pi(t_{init})}{\gamma}$, $M_1(t_{init}) = 1$ cell and $M_{i=2...n}(t_{init}) = E(t_{init}) = 0$. We fixed parameter $\gamma = 15$ day$^{-1}$ (56), $\delta E = 1$ day$^{-1}$, and $\phi = 100$ cells. We assumed this value of $\phi$ because of the low percentage (~2%) of activated T cells that start growing at the moment of viral load drop (58). We estimated the remaining parameters including the time of infection $t_{init}$.

To determine the most parsimonious model among the instances for the available SARS-CoV-2 shedding data, we computed the log-likelihood (log $L$) and the Akaike Information Criteria (AIC=$-2$log$L$+$2m$, where $m$ is the number of parameters estimated). We assumed a model has similar support from the data if the difference between its AIC and the best model (lowest) AIC is less than two (59).
We also explored the antiviral effect of a hypothetical bNAb using the form \( \epsilon(t) = \frac{C_d(t)}{C_d(t) + EC_{50}} \) and varied values of EC50 between 1 and 1000 \( \mu \text{M} \). Finally, we modeled the potential antiviral effect of immunotherapies by enhancing the early death rate of infected cells (\( \delta \)) by a factor of 50%, 100% and 200%.

### Modeling the emergence of resistance to remdesivir

We adapted the model in Eq. 1 to allow for the emergence of resistance to RDV. We base the modifications on the fact that two separate mutations may induce partial resistance to RDV in SARS CoV-1 which in turn leads to a less fit virus (38). In the case of SARS CoV-1, two single mutations can induce to a less sensitive virus with 2.4- and 5.0-fold increase in the RDV EC50. When the combined mutations emerged, it mediated a 5.6-fold increase in the RDV EC50. We included these findings in the model by assuming that infected cells (\( I_2 \)) that produce sensitive virus (\( V_2 \)) can transition into infected cells (\( I_1 \) and \( I_2 \)) that produce less sensitive virus (\( V_1 \) and \( V_2 \)), due to one mutation during the viral replication cycle. These two viral populations have an increased EC50 (2.4- and 5-fold higher). Similarly, we assumed that \( I_1 \) and \( I_2 \) can transition into infected cells that produce a more resistant strain \( V_{12} \) (with 5.6-fold higher EC50) after another mutation. We also allowed for reversal mutation events. We assumed a mutation probability of \( \mu = 10^{-5} \) per infection event. Under these assumptions total viral load is defined as \( V = V_1 + V_2 + V_{12} \) and total number of infected cells as \( I = I_1 + I_2 + I_{12} \). With these modifications the model becomes,

\[
\frac{dS}{dt} = \beta VS
\]

\[
\frac{dI_1}{dt} = (1-2\mu)\beta SV_1 + \mu \beta S(V_1 + V_2) - \delta I_1 - \frac{mE^r}{E^r + \phi^r} I_1,
\]

\[
\frac{dI_{12}}{dt} = \mu \beta SV_{12} + (1-2\mu)\beta SV_{12} - \delta I_{12} - \frac{mE^r}{E^r + \phi^r} I_{12},
\]

\[
\frac{dI_2}{dt} = \mu \beta SV_2 + (1-2\mu)\beta SV_{12} - \delta I_2 - \frac{mE^r}{E^r + \phi^r} I_2,
\]

\[
\frac{dV_1}{dt} = \pi (1-\epsilon_1) I_1 - \gamma V_1
\]

\[
\frac{dV_2}{dt} = \pi (1-\epsilon_2) I_2 - \gamma V_2
\]

\[
\frac{dV_{12}}{dt} = \pi (1-\epsilon_{12}) I_{12} - \gamma V_{12}
\]
2. D. Wang


ACKNOWLEDGMENTS

We are grateful to study participants from around the globe who donated critical virologic data early during the pandemic. Funding: This study was supported by Fred Hutchinson Cancer Research Center faculty discretionary funds and by National Institute of Allergy and Infectious Diseases (grant # 5R01AI121129-05). Author contributions: J.T.S. conceived the study, A.G. and E.F.C. assembled data, wrote all code, performed all calculations and derivations, ran the models, and analyzed output data. J.T.S. wrote the manuscript with contributions from all other authors. Competing interests: The authors declare no competing interests. J.T.S. has on the trial planning committee for a Gilead funded trial of remdesivir but is not reimbursed for this activity. Data and materials availability: The original data and code is shared at https://github.com/ashish2goyal/SARS-COV-2_Within_host_Viral_dynamics

SUPPLEMENTARY MATERIALS

advances.sciencemag.org/cgi/content/full/sciadv.abc7112/DC1

Submitted 8 May 2020

Accepted 7 October 2020

Published First Release 23 October 2020

10.1126/sciadv.abc7112
Fig. 1. Mathematical model recapitulation of untreated SARS-CoV-2 kinetics. A. Mathematical model schematic including infection of susceptible cells (S), production of virus by (V) by infected cells (I), an early density-dependent immune response governed by exponent k, and a mounting T cell response with sequential populations of T cells (M1, M2, and E) which kill infected cells when above a certain threshold. B. Model fit to individual data. Shapes are individual viral loads and lines are model load projections. S = Singapore; G = Germany; K = South Korea; F = France.
Fig. 2. Early innate and late acquired killing rates of SARS-CoV-2 infected cells. Model projections of rates in 15 participants who cleared viral shedding. **A.** Per cell death rate mediated by innate responses (blue) and acquired immune responses (green). **B.** Total death rate mediated by innate responses (blue) and acquired responses (green).
Fig. 3. Projected pharmacokinetics and pharmacodynamics of remdesivir therapy. A. Complete model of remdesivir (RDV) including plasma levels of parent drug, intracellular levels of the active component (NTP) and antiviral efficacy of drug according to NTP concentration. B. Projections of plasma RDV levels and intracellular NTP in PBMCs. Datapoints from non-human primate experiments are dots while lines are model projections. C. Simulated concentrations of the parent compound and intracellular levels of the active compound with a loading dose of 200 mg IV followed by 9 daily doses of 100 mg IV. D. Pharmacodynamic projections of antiviral efficacy according to drug concentration assuming different values for the in vivo EC50 of the drug. E. Projected antiviral effects using combined pharmacokinetic and pharmacodynamic models at different assumed drug potencies.
Fig. 4. Treatment projections of a 10-day remdesivir course assuming different potency and timing of treatment. Each set of simulations is performed under assumptions of high, medium and low potency (EC50=0.8, 8 and 80 µM respectively). Treatment initiation at timepoints generally consistent with A. hospitalization (day 10 after first positive sample), B. first symptoms (day 5 after first positive sample), C. pre-symptomatic post-peak phase (day 2 after first positive sample) and D. pre-symptomatic pre-peak phase (day 0). Overall, early potent treatment limits duration of infection. Prolonged shedding is predicted as a possibility with sub-potent, early initiation of therapy due to inadequate activation of immunity.
Fig. 5. Predictors of SARS-CoV-2 treatment outcomes with remdesivir. Heatmaps comparing variance in drug potency measured by in vivo EC50 (x-axis) and timing of treatment initiation (y-axis) for A. Shedding duration, B. viral load area under the curve (AUC) and C. extent of T cell response required for viral elimination. Potent therapy within the first 5 days of infection limits shedding duration and the extent of the T cell response. However, only extremely early therapy during the pre-symptomatic phase of infection dramatically lowers viral AUC. Sub-potent therapy given during the extremely early pre-symptomatic stage may extend shedding duration at lower viral loads by limiting the immune response.
Fig. 6. Projections of remdesivir drug resistance during therapy. Simulations are with assumed high potency (EC50=0.8 uM) and the assumption that mutants confer partial drug resistance. Treatment initiation is at timepoints generally consistent with hospitalization (day 10 after first positive sample), first symptoms (day 5 after first positive sample), pre-symptomatic post-peak phase (day 2 after first positive sample) or pre-symptomatic pre-peak phase (day 0). A, Projections of no treatment, treatment with no assumed drug resistance, and treatment with assumed drug resistance. B, Projections of assumed drug resistance with trajectories of sensitive strains, single mutants and double mutants. Here, DOT represents the day of the start of the treatment.
Fig. 7. Projections of remdesivir drug resistance during therapy. Simulations are with moderate potency (EC50=8.0 μM) and the assumption that mutants confer partial drug resistance. Treatment initiation is at timepoints generally consistent with hospitalization (day 10 after first positive sample), first symptoms (day 5 after first positive sample), pre-symptomatic post-peak phase (day 2 after first positive sample) or pre-symptomatic pre-peak phase (day 0). A. Projections of no treatment, treatment with no assumed drug resistance, and treatment with assumed drug resistance. B. Projections of assumed drug resistance with trajectories of sensitive strains, single mutants and double mutants. Here, DOT represents the day of the start of the treatment.
Fig. 8. Projected pharmacokinetics and pharmacodynamics of selinexor therapy. A. Complete model of selinexor including plasma levels, PBMC levels, inhibition of XPO1 mediated cellular export of viral proteins, and inhibition of viral replication in a dose-dependent fashion. B. Single dose models drug levels (line) reproduce observed datapoints at different doses. C. Projected PBMC levels assuming low and high selinexor absorption rates. D. Predicted fold-change in compensatory XPO1 mRNA expression after a single dose with model fits to data. E. Projected plasma (black), and PBMC (red, dashed = high absorption and solid = low absorption) selinexor levels with three times weekly dosing for 4 weeks. F. Pharmacodynamic projections of antiviral efficacy according to drug concentration assuming different values for the in vivo EC50 of the drug. G. Predicted fold-change in compensatory XPO1 mRNA expression after multiple doses, and H. Projected antiviral effects using combined pharmacokinetic and pharmacodynamic models at different assumed drug potencies.
Fig. 9. Projected pharmacokinetics and pharmacodynamics of neutralizing antibody therapy. A. Complete bi-compartment model of broadly neutralizing antibody (bNAb) therapy with lowering of viral infectivity according to antibody concentration. B. Projections of plasma bNAb levels from simulations of VRC01 treatment. C. Pharmacodynamic projections of antiviral efficacy according to antibody concentration assuming different values for the in vivo EC50. D. Combination simulations of pharmacokinetic and pharmacodynamic models demonstrating antiviral activity as a function of time.
**Fig. 10. Treatment projections of cytolytic immunotherapy assuming different potency and timing of treatment.** Each set of simulations is performed under assumptions of high, medium and low potency based on multiplicative effect on infected cell death rate. Treatment initiation is at timepoints generally consistent with **A.** hospitalization (day 10 after first positive sample), **B.** first symptoms (day 5 after first positive sample), **C.** presymptomatic post-peak phase (day 2 after first positive sample) and **D.** presymptomatic pre-peak phase (day 0). Overall, early potent treatment limits duration of infection but extremely early therapy fails. Prolonged shedding is predicted as a possibility with sub-potent, early initiation of therapy due to inadequate activation of immunity.
Potency and timing of antiviral therapy as determinants of duration of SARS-CoV-2 shedding and intensity of inflammatory response
Ashish Goyal, E. Fabian Cardozo-Ojeda and Joshua T. Schiffer

published online October 23, 2020