

## Supplementary Materials for **Scale-dependent erosional patterns in steady-state and transient-state landscapes**

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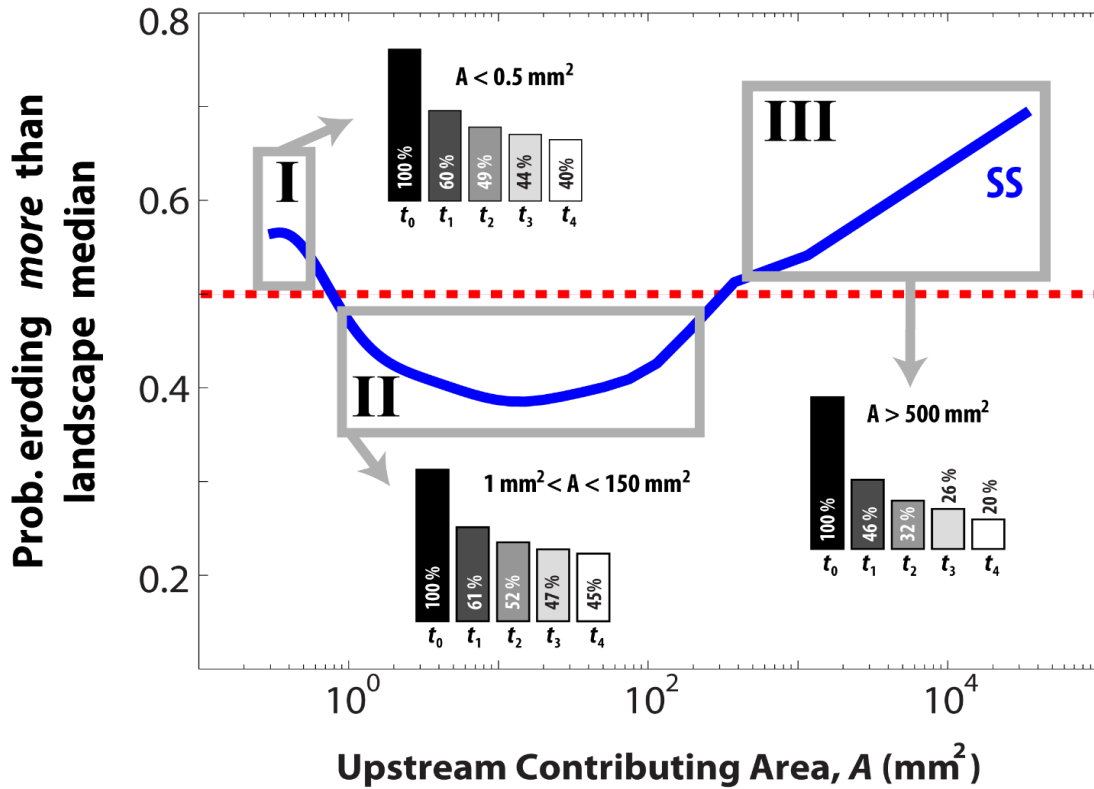
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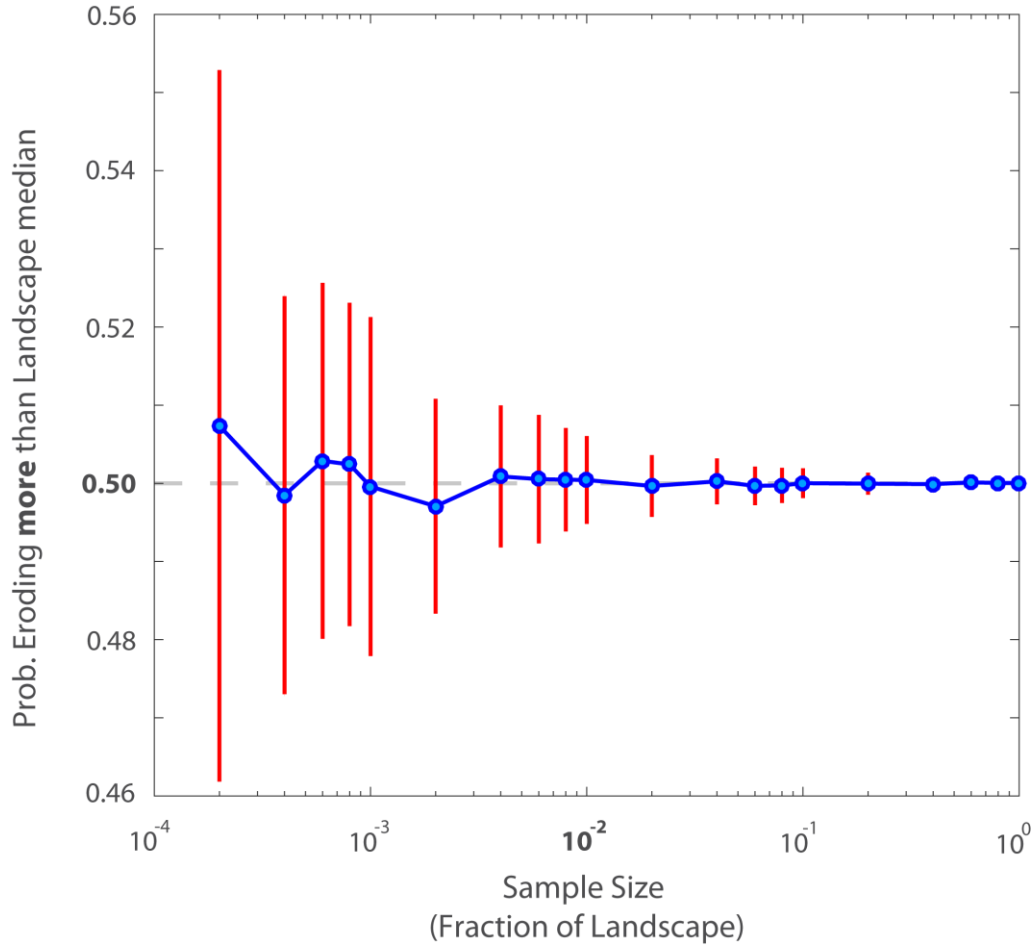
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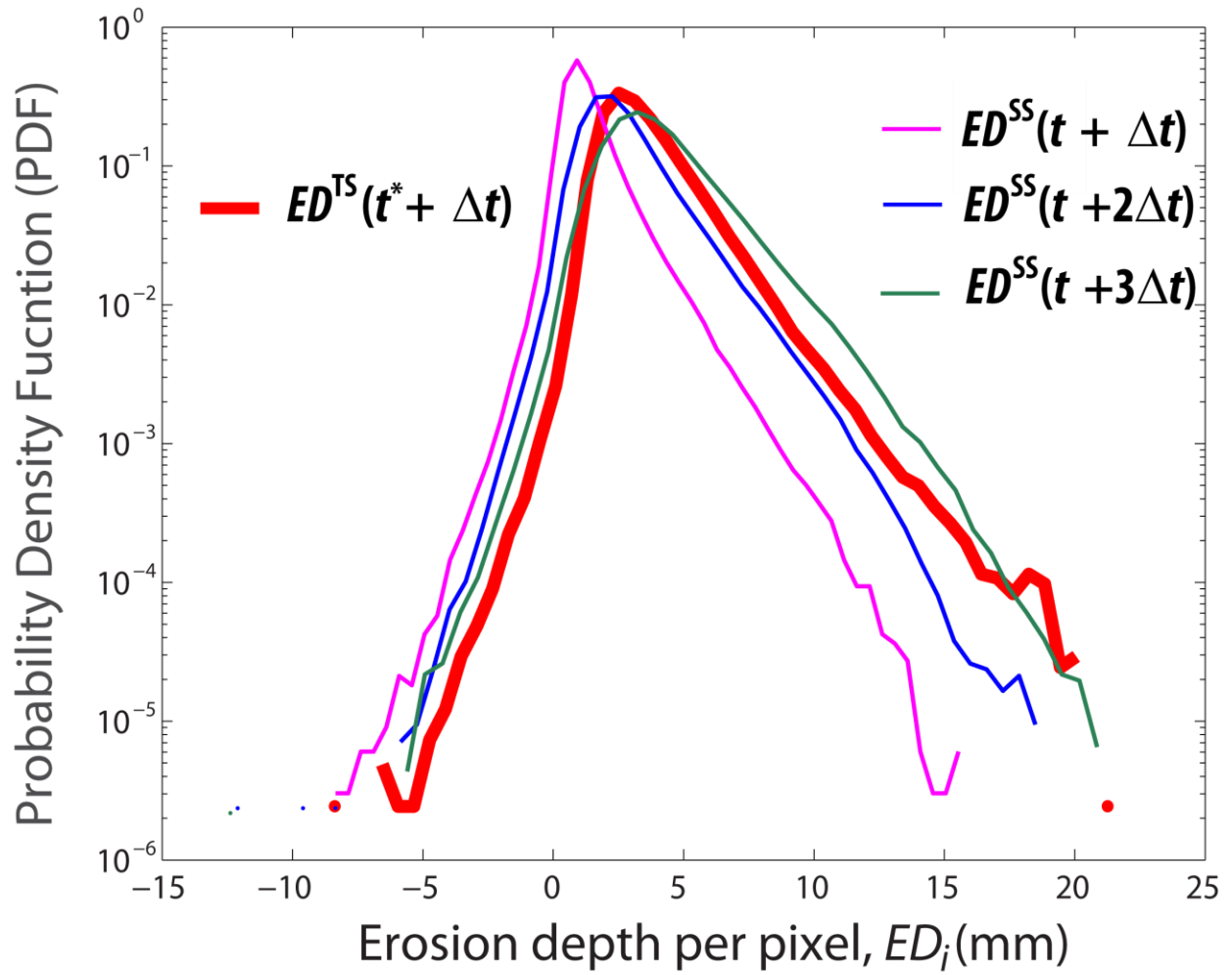
## Scale-dependent erosional patterns in SS and TS landscapes



**fig. S1. Dynamic landforms at SS.** The shape of the E50-area curve reveals that the likelihood of eroding more (or less) than the median of the landscape is nonlinearly related to the upstream contributing area,  $A$ . We examine the dynamic nature of steady-state landscapes within three ranges of upstream contributing areas: (I)  $A < 0.5$  mm<sup>2</sup>, with a higher likelihood of eroding more than the median of the landscape; (II)  $1 \text{ mm}^2 < A < 150 \text{ mm}^2$ , with a lower likelihood of eroding more than the landscape median; (III)  $A > 500 \text{ mm}^2$ , with a higher likelihood of eroding more than the landscape median. We identify at a given time ( $t_0$ ) the location of all the pixels on the landscape within each of the three ranges defined above (100%). For each subsequent topography (measured 5 min apart), we compute the percentage of pixels on those locations, which are still characterized by  $A$  in the same interval as initially defined. The inset plots show that, in each area range, a significant percentage of pixels change their upstream contributing areas over time, illustrating the dynamic nature of steady-state landscapes.



**fig. S2. Estimation of the probability of erosion larger than the landscape median at SS for different sample sizes.** Blue circles correspond to the estimated probability of eroding more than the median of the landscape (Y axis) by using 100 randomly selected samples of a given size (X axis). The red lines correspond to standard deviations estimated from the 100 samples. Note that to construct the E50-area curve we used 100 bins, which have a constant sample size equal to 0.01 fraction of the landscape. From the results corresponding to sample size equal to  $10^{-2}$  shown in this figure, we can conclude that the patterns depicted by the E50-area curves (see Fig. 3 and 4 in the main text) are statistically significant.



**fig. S3. Comparison of the SS and TS landscapes in terms of the aggregate statistics of ED.**

Probability density functions (PDFs) of erosion depth per pixel,  $ED_i$ , in the TS landscape, subject to a five-fold increase in precipitation intensity during 5 minutes ( $\Delta t$ ) starting at time  $t^*$  (red curve), and the SS landscape during 5 (magenta), 10 (blue), and 15 (green) minutes.